

# Agonist-dependent Phosphorylation of the Inositol 1,4,5-Trisphosphate Receptor

## *A Possible Mechanism for Agonist-specific Calcium Oscillations in Pancreatic Acinar Cells*

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**ABSTRACT** The properties of inositol 1,4,5-trisphosphate (IP<sub>3</sub>)-dependent intracellular calcium oscillations in pancreatic acinar cells depend crucially on the agonist used to stimulate them. Acetylcholine or carbachol (CCh) cause high-frequency (10–12-s period) calcium oscillations that are superimposed on a raised baseline, while cholecystokinin (CCK) causes long-period (>100-s period) baseline spiking. We show that physiological concentrations of CCK induce rapid phosphorylation of the IP<sub>3</sub> receptor, which is not true of physiological concentrations of CCh. Based on this and other experimental data, we construct a mathematical model of agonist-specific intracellular calcium oscillations in pancreatic acinar cells. Model simulations agree with previous experimental work on the rates of activation and inactivation of the IP<sub>3</sub> receptor by calcium (DuFour, J.-F., I.M. Arias, and T.J. Turner. 1997. *J. Biol. Chem.* 272:2675–2681), and reproduce both short-period, raised baseline oscillations, and long-period baseline spiking. The steady state open probability curve of the model IP<sub>3</sub> receptor is an increasing function of calcium concentration, as found for type-III IP<sub>3</sub> receptors by Hagar et al. (Hagar, R.E., A.D. Burgstahler, M.H. Nathanson, and B.E. Ehrlich. 1998. *Nature.* 396:81–84). We use the model to predict the effect of the removal of external calcium, and this prediction is confirmed experimentally. We also predict that, for type-III IP<sub>3</sub> receptors, the steady state open probability curve will shift to lower calcium concentrations as the background IP<sub>3</sub> concentration increases. We conclude that the differences between CCh- and CCK-induced calcium oscillations in pancreatic acinar cells can be explained by two principal mechanisms: (a) CCK causes more phosphorylation of the IP<sub>3</sub> receptor than does CCh, and the phosphorylated receptor cannot pass calcium current; and (b) the rate of calcium ATPase pumping and the rate of calcium influx from the outside the cell are greater in the presence of CCh than in the presence of CCK.

**KEY WORDS:** inositol 1,4,5-trisphosphate receptor • phosphorylation • protein kinase A • mathematical model • calcium oscillations

### introduction

The production of the intracellular signaling factor inositol 1,4,5-trisphosphate (IP<sub>3</sub>)<sup>1</sup> and the subsequent release of Ca<sup>2+</sup> stored in intracellular organelles is a fundamental cellular signaling function (Berridge, 1997). The form of the resultant change in the intracellular free Ca<sup>2+</sup> con-

centration ([Ca<sup>2+</sup>]<sub>i</sub>) is highly variable. Specific, well-characterized response types include a single, large increase in [Ca<sup>2+</sup>]<sub>i</sub>, which may virtually deplete the stores, and smaller, maintained oscillations of [Ca<sup>2+</sup>]<sub>i</sub> (Berridge, 1990). Often both patterns may be observed in a single cell type, depending on the agonist concentration.

The release of Ca<sup>2+</sup> by IP<sub>3</sub> occurs through the activation of a specific receptor for IP<sub>3</sub>, which is located on the endoplasmic reticulum (ER) surface, and which is also a functional calcium channel (Bezprozvanny and Ehrlich, 1995; Taylor and Traynor, 1995; Joseph, 1996; Yoshida and Imai, 1997; Taylor, 1998). In addition to its IP<sub>3</sub> binding site (at the NH<sub>2</sub>-terminal end) and its pore-forming region (the COOH-terminal end, containing six membrane-spanning regions), the IP<sub>3</sub> receptor (IP<sub>3</sub>R) also contains a large regulatory domain between the NH<sub>2</sub>- and COOH-terminal regions. A number of cytosolic factors have been suggested to modulate IP<sub>3</sub>R activity, including, but not restricted to, PKA, PKC,

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<sup>1</sup>*Abbreviations used in this paper:* Ach, acetylcholine; CaMK-II, Ca<sup>2+</sup>-calmodulin kinase II; CCK, cholecystokinin; CPA, cyclopiazonic acid; ER, endoplasmic reticulum; IP<sub>3</sub>, inositol 1,4,5-trisphosphate; IP<sub>3</sub>R, IP<sub>3</sub> receptor.

Ca<sup>2+</sup>-calmodulin kinase II (CaMK-II), adenine, and possibly guanine nucleotides. These additional factors may permit the wide range of response types that are seen for IP<sub>3</sub>-induced Ca<sup>2+</sup> release.

In addition to factors such as kinases modulating IP<sub>3</sub>R activity, Ca<sup>2+</sup> itself plays a fundamental role. A number of studies have shown that the steady state open probability of the type-I IP<sub>3</sub>R displays a bell-shaped dependence on [Ca<sup>2+</sup>]<sub>i</sub>, with a peak at approximately [Ca<sup>2+</sup>]<sub>i</sub> = 300 nM (Bezprozvanny and Ehrlich, 1995; Taylor and Traynor, 1995; Joseph, 1996), while for type-III IP<sub>3</sub> receptors the open probability curve is a monotonically increasing function of [Ca<sup>2+</sup>]<sub>i</sub> (Hagar et al., 1998). However, the steady state behavior of the receptor is much less important than the dynamic response of the receptor to a sudden increase of either [Ca<sup>2+</sup>]<sub>i</sub> or [IP<sub>3</sub>]. When exposed to a sudden change in [Ca<sup>2+</sup>]<sub>i</sub> or [IP<sub>3</sub>], the receptor responds by a transient increase in open probability, followed by adaptation or recovery, to a lower level (Finch et al., 1991; Dufour et al., 1997; Marchant and Taylor, 1998). Direct injection of IP<sub>3</sub>, or the use of nonhydrolyzable IP<sub>3</sub> analogues, has shown that in mouse pancreatic acinar cells oscillations of [Ca<sup>2+</sup>]<sub>i</sub> can occur when the IP<sub>3</sub> concentration is constant (Wakui et al., 1989; Berridge and Potter, 1990). Thus, dynamic regulation of the receptor by Ca<sup>2+</sup> may represent the mechanism by which oscillations of [Ca<sup>2+</sup>]<sub>i</sub> arise, with Ca<sup>2+</sup> initially promoting its own release, and then secondarily inhibiting further release. In the DISCUSSION, we discuss the possible effects on the model of changing IP<sub>3</sub> concentrations.

A number of mathematical models have been developed to simulate IP<sub>3</sub>-induced Ca<sup>2+</sup> release (De Young and Keizer, 1992; Atri et al., 1993; Sneyd et al., 1995; Tang et al. 1996), although, to date, all models have been based on the properties of the type-I receptor. In the model of De Young and Keizer (1992), each subunit of the tetrameric IP<sub>3</sub>R contains one binding site for IP<sub>3</sub> and two binding sites for Ca<sup>2+</sup>, an activating site and an inactivating state. It was assumed that Ca<sup>2+</sup> flux occurred only when the IP<sub>3</sub> binding site and the activating Ca<sup>2+</sup> binding site were occupied, and the Ca<sup>2+</sup> inactivating site was unoccupied. This formulation resulted in an eight-state model, only one of which was a conducting state. With rate constants for interconversion between the eight states chosen, where possible, to correspond to experimental values, this model displayed oscillatory behavior over a range of [IP<sub>3</sub>] (De Young and Keizer, 1992). A fundamental feature of this model, necessary to allow oscillations to occur, is that IP<sub>3</sub> and Ca<sup>2+</sup> binding to the activation site are fast processes, whereas Ca<sup>2+</sup> binding to the inhibitory site is a slow process. Other models of IP<sub>3</sub>R kinetics (Atri et al., 1993; Sneyd et al., 1995) are based on the same premise of fast activation and slow inhibition by Ca<sup>2+</sup>, and Tang

et al. (1996) showed that these are essentially equivalent formulations. A model of [Ca<sup>2+</sup>]<sub>i</sub> dynamics in pituitary gonadotroph cells (Li et al., 1994, 1997) is perhaps the most highly developed of these in terms of the specific cellular mechanisms controlling [Ca<sup>2+</sup>]<sub>i</sub> and equivalence of the model behavior to experimental single cell data.

Experimental data on the relative rates of activation and inactivation of the IP<sub>3</sub>R by Ca<sup>2+</sup> is consistent with inactivation being a slower process (Parker and Ivorra, 1990). However, careful analysis of data with higher kinetic resolution (Finch et al., 1991; Dufour et al., 1997; Marchant et al., 1997; Marchant and Taylor, 1998) suggests that the difference between the rates of activation and inactivation is not as great as is typically used in mathematical models. Furthermore, despite the fact that inactivation is apparently too slow in the models, the models are unable to reproduce long-period, baseline oscillations (up to 2 min or longer in period) observed in cells such as hepatocytes (Kawanishi et al., 1989) and pancreatic acinar cells (Yule et al., 1991). Recent models have addressed the issue of long-period oscillations (Dupont and Swillens, 1996; Laurent and Claret, 1997), but their relevance to any particular cell type is, as yet, unclear.

From the point of view of modeling Ca<sup>2+</sup> oscillations and waves, pancreatic acinar cells present particular difficulties. Firstly, in response to different agonists, pancreatic cells exhibit markedly different Ca<sup>2+</sup> responses (Petersen et al., 1991b; Yule et al., 1991; Lawrie et al., 1993; Thorn et al., 1993b). Application of acetylcholine (ACh) to pancreatic acinar cells results in the generation of [Ca<sup>2+</sup>]<sub>i</sub> oscillations that are roughly sinusoidal with a frequency of ~4–6/min. The [Ca<sup>2+</sup>]<sub>i</sub> oscillations are superimposed on a raised baseline such that [Ca<sup>2+</sup>]<sub>i</sub> does not fall to basal levels before the generation of the next peak (Yule et al., 1991). In contrast, the [Ca<sup>2+</sup>]<sub>i</sub> response to cholecystokinin (CCK) is very different, consisting of baseline spikes of much longer period.

Despite these differences, there is much evidence that both types of oscillations result from agonist-dependent activation of phospholipase C, and the resulting increase in intracellular [IP<sub>3</sub>] (see DISCUSSION). How might these two very different patterns of Ca<sup>2+</sup> release occur, with apparently the same basic intracellular processes? In particular, how do the long baseline spikes observed with CCK occur, given that [IP<sub>3</sub>] is thought to be maintained above basal levels throughout the period of stimulation, whereas [Ca<sup>2+</sup>]<sub>i</sub>, which initially provides the negative feedback signal to end Ca<sup>2+</sup> flux from the stores, has returned to its basal values long before the next spike occurs? In studying these questions, it is important to keep in mind that pancreatic acinar cells contain a preponderance of type-III IP<sub>3</sub> receptors (Wojcikiewicz, 1995), and thus any model to explain the observed oscillations should

be based on data from the correct receptor subtype wherever possible. Fortunately, data on the steady state properties of type-III IP<sub>3</sub> receptors have recently become available, although their adaptational and time-dependent properties are still unknown in detail.

Our goal is to understand the mechanisms underlying these different oscillatory patterns and provide a single explanation for these seemingly diverse phenomena. Of course, such an explanation can be simplistic at best and cannot take into account all the complexities of the real cell. Nevertheless, it will provide a framework to help us understand how a set of relatively simple cellular interactions can result in diverse and complex behavior. We begin by showing (experimentally) that in mouse and rat pancreatic acinar cells physiological concentrations of CCK cause rapid phosphorylation of the type-III IP<sub>3</sub>R, but physiological concentrations of ACh do not. Assuming that the phosphorylated receptor does not pass Ca<sup>2+</sup> current (see DISCUSSION), it follows that the rate at which the IP<sub>3</sub>R recovers from inactivation depends crucially on the agonist. Secondly, we show that the rate of Ca<sup>2+</sup> removal from the cytoplasm is an order of magnitude slower after application of CCK than after application of ACh. These data are then incorporated into a model of the type-III IP<sub>3</sub>R, and thus into a whole-cell model of the Ca<sup>2+</sup> response. The model provides a unified explanation of seemingly disparate results; it agrees with the rates of activation and inactivation of the IP<sub>3</sub>R by Ca<sup>2+</sup>, as measured by Finch et al. (1991) and Dufour et al. (1997), but can nevertheless produce oscillations of very long period and generate oscillations of the two observed types. Furthermore, the steady state open probability of the model type-III IP<sub>3</sub> receptor is an increasing function of Ca<sup>2+</sup>, as found experimentally by Hagar et al. (1998), thus showing that such monotonic steady state curves are consistent with oscillatory behavior, a fact that is not always appreciated. Predictions of the model are then tested, and confirmed, experimentally.

## methods

### Materials

Fura-2/AM was purchased from Molecular Probes, Inc., collagenase (CLSPA grade) from Worthington Biochemicals, bovine serum albumin (fraction V) from ICN Immunobiologicals, and minimal essential amino acid supplement from GIBCO BRL. [<sup>32</sup>P]orthophosphate (9,000 Ci/mmol) was obtained from Dupont NEN. Monoclonal antisera directed against the type-III inositol 1,4,5-trisphosphate receptor was obtained from Transduction Laboratories. All other materials were obtained from Sigma Chemical Co.

### Preparation of Pancreatic Acini

Acini were prepared by methods previously described (Williams et al., 1978; Yule et al., 1996). In brief, pancreata were excised

from freely fed adult male Sprague-Dawley rats (200–250 g) or mice. Acini were prepared by enzymatic digestion with purified collagenase, followed by mechanical shearing. Acini were then filtered through 150 μm Nitex mesh, purified by sedimentation through 4% BSA in HEPES ringer, and then suspended in a physiological salt solution containing 10 mg/ml bovine serum albumin, 0.1 mg/ml soybean trypsin inhibitor, and (mM): 137 NaCl, 4.7 KCl, 0.56 MgCl<sub>2</sub>, 1.28 CaCl<sub>2</sub>, 1.0 Na<sub>2</sub>HPO<sub>4</sub>, 10 HEPES, 2 L-glutamine, 5.5 D-glucose, essential amino acids. The pH was adjusted to 7.4 and equilibrated with 100% O<sub>2</sub>.

### Measurement of [Ca<sup>2+</sup>]<sub>i</sub>

Isolated acini were incubated with 2.5 μM fura-2/AM at ambient temperature for 30 min, and then washed and resuspended in fresh physiological salt solution without BSA. For measurement of [Ca<sup>2+</sup>]<sub>i</sub>, fura-2-loaded acini were transferred to a chamber, mounted on the stage of an Axiovert 35 microscope (Carl Zeiss, Inc.), and continuously superfused at 1 ml/min with PSS without BSA. Solution changes were rapidly accomplished by means of a valve attached to an eight-chambered superfusion reservoir, which was maintained at 37°C. Determination of [Ca<sup>2+</sup>]<sub>i</sub> was performed using digital imaging microscopy with an ATTOFLUOR ratiovision system (ATTO Inc.) as previously described (Yule et al., 1996). Briefly, excitation at 340/380 nm was alternately achieved by a computer controlled filter and shutter system and the resultant emission at 505 nm was recorded at the rates indicated in the figures by an intensified CCD camera, and subsequently digitized. Mean gray values obtained by excitation at 340 and 380 nm, in user-defined areas of interest, were used to compute 340/380 ratios. Calibration of fluorescent ratio signals was accomplished as previously described according to the equation of Grynkiewicz et al. (1985) by comparing the fluorescence of known standard Ca<sup>2+</sup> buffers containing fura-2.

### Assessment of Phosphorylation of the Type-III IP<sub>3</sub> Receptor

Acini were labeled with 0.3 mCi/ml <sup>32</sup>PO<sub>4</sub> for 2 h in HEPES ringer devoid of added phosphate. Aliquots of labeled acinar cells were then treated as indicated. At the end of the incubations, the acini were rapidly centrifuged in a microcentrifuge and the pellets were resuspended in ice-cold lysis buffer containing 100 mM NaF, 50 mM Tris-HCl, pH 7.4, 150 mM NaCl, 10 mM EDTA, 1 mM benzamide, 1% Triton X-100, 10 μg/ml leupeptin, and 10 μg/ml pepstatin, at pH 7.4). The homogenates were then sonicated. After 30 min on ice, the samples were precleared by addition of 100 μl of protein A-agarose beads and rotation for 2 h at 4°C. The protein A beads were removed by centrifugation and the protein content of the samples was assayed. Type-III IP<sub>3</sub>R was immunoprecipitated from the samples of equal protein by incubation with 1 μg antibody/mg of protein (Transduction Laboratories) for 3 h. After incubation, the beads were washed five times with the lysis buffer by centrifugation and resuspension. After the final wash, the beads were boiled in Laemmli buffer and immunoprecipitated proteins separated by electrophoresis on 5% SDS-PAGE gels. The gel was dried and exposed to a Phosphor-imager intensifying screen (Bio-Rad Laboratories) for visualization and analyzed by molecular analyst software for quantification (Bio-Rad Laboratories).

## results

*Secretagogue phosphorylation of the type-III IP<sub>3</sub> receptor.* Aliquots of acini (in duplicate), metabolically labeled with <sup>32</sup>P, were stimulated with secretagogues for 2 min and

the extent of phosphorylation of the receptor was assessed by immunoprecipitating the receptor, separation on SDS-PAGE, and then autoradiography. Acini were initially treated with varying concentrations of CCK. In unstimulated acini, phosphorylation of one major band of  $\sim 300$  kD, corresponding to the type-III IP<sub>3</sub>R, could be detected. An increase in the degree of phosphorylation could be demonstrated at 10 pM CCK ( $170 \pm 15\%$  above basal) and reached a maximum at 100 nM CCK ( $252 \pm 23\%$  of control). Phosphorylation of the receptor was not significantly greater at 1 or 10 nM CCK ( $n = 4$  rat and 2 mouse preparations gave qualitatively similar results). It should be noted that the onset and maximum phosphorylation of the receptor achieved coincides with concentrations of CCK that can be demonstrated to induce calcium oscillations (Yule et al., 1991, 1993). Fig. 1 shows a typical experiment. The extent of receptor phosphorylation was also investigated upon stimulation by the muscarinic agonist, carbachol. In this series of experiments, an increased phosphorylation of the type-III IP<sub>3</sub>R was also consistently observed 2 min after stimulation with agonist. Phosphorylation could be detected at 1  $\mu$ M CCh ( $160 \pm 22\%$ ) and reached a peak at 10  $\mu$ M ( $203 \pm 28\%$  of control). In contrast to stimulation by CCK, no significant phosphorylation of the receptor was observed at concentrations of CCh below 1  $\mu$ M, concentrations that can be demonstrated to induce an oscillatory calcium signal (Yule et al., 1991;  $n = 3$  rat and 2 mouse preparations gave quantitatively similar results). A typical experiment is shown in Fig. 2.

It is known that, in pancreatic acinar cells, CCK activates both the adenylate cyclase pathway as well as the phospholipase C pathway, while ACh activates only the latter pathway (Schulz, 1989; Petersen and Wakui, 1990). Thus, a plausible working hypothesis is that the CCK-induced receptor phosphorylation is caused by the activation of PKA, a pathway that is not stimulated by ACh, or at least not to the same extent.

**Phosphorylation of the type-III IP<sub>3</sub> receptor by second messengers.** To investigate the mediator generated upon agonist stimulation that results in phosphorylation of the type-III IP<sub>3</sub>R, duplicate aliquots of acini were incubated for 5 min with agents known to activate or be a mediator in discrete second-messenger pathways: acini were incubated in either cyclopiazonic acid (CPA), which leads to an elevation of  $[Ca^{2+}]_i$  by inhibition of the  $Ca^{2+}$ -ATPase present on intracellular calcium stores, TPA, an activator of protein kinase C, or CPT-cAMP, a cell-permeable cAMP analog. In three experiments ( $n = 2$  rat and 1 mouse preparation) no enhanced phosphorylation of the type-III IP<sub>3</sub>R was ever observed from acini incubated with either TPA or CPA, indicating that a calcium-dependent kinase or protein kinase C is apparently not responsible for phosphorylation of the receptor. A marked increase in phosphorylation was, how-

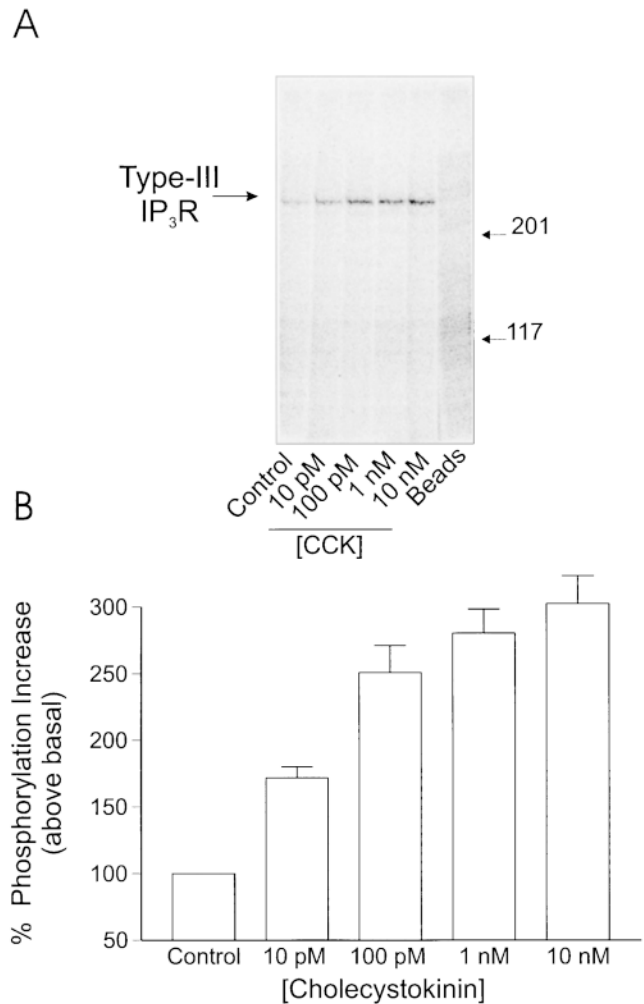
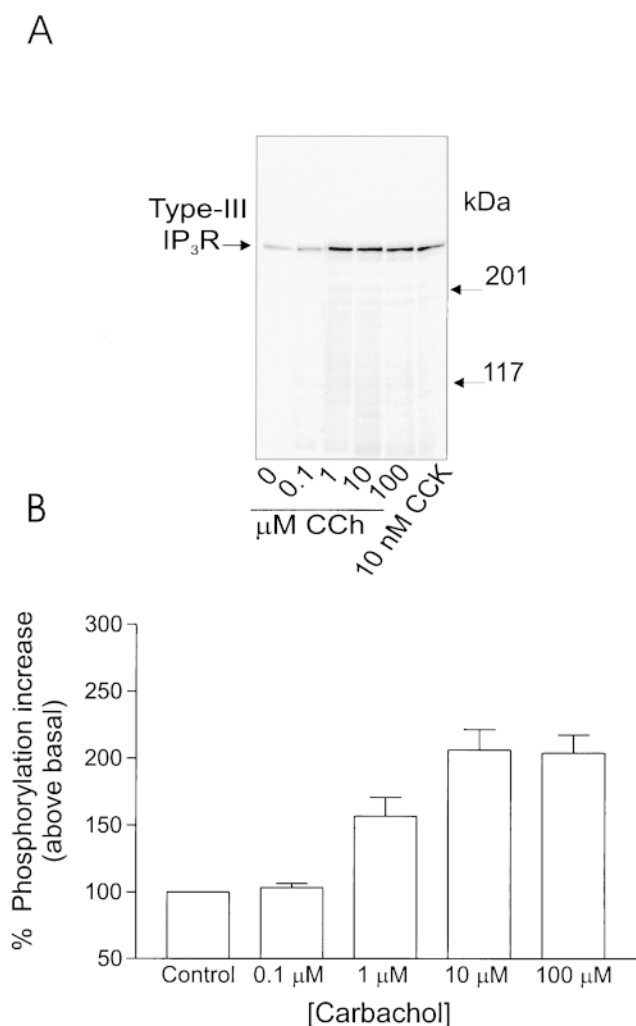


FIGURE 1. Phosphorylation of type-III IP<sub>3</sub> receptor after stimulation by cholecystokinin in rat pancreatic acini: acini were prepared and samples were processed as detailed in the METHODS. (A) In acini under control conditions, a single phosphorylated band was observed at  $\sim 300$  kD, corresponding to the type-III IP<sub>3</sub> receptor. On stimulation by CCK, the intensity of this band increased; the increase was detected at 10 pM CCK and reached a maximum at 100 pM CCK. These concentrations of CCK are physiologically relevant and induce oscillatory  $[Ca^{2+}]_i$  signals. In the extreme right lane, samples were processed in an identical manner except that the immunoprecipitating antisera were omitted. (B) Pooled data (mean  $\pm$  SEM) from at least three independent experiments, where samples were run in duplicate.

ever, always observed when the acini were incubated with CPT-cAMP. The extent of phosphorylation,  $>427 \pm 52\%$  above basal, was greater than observed with phospholipase C-coupled agonists. These data indicate that a cAMP-dependent pathway is capable of phosphorylating the receptor. A typical experiment is shown in Fig. 3.

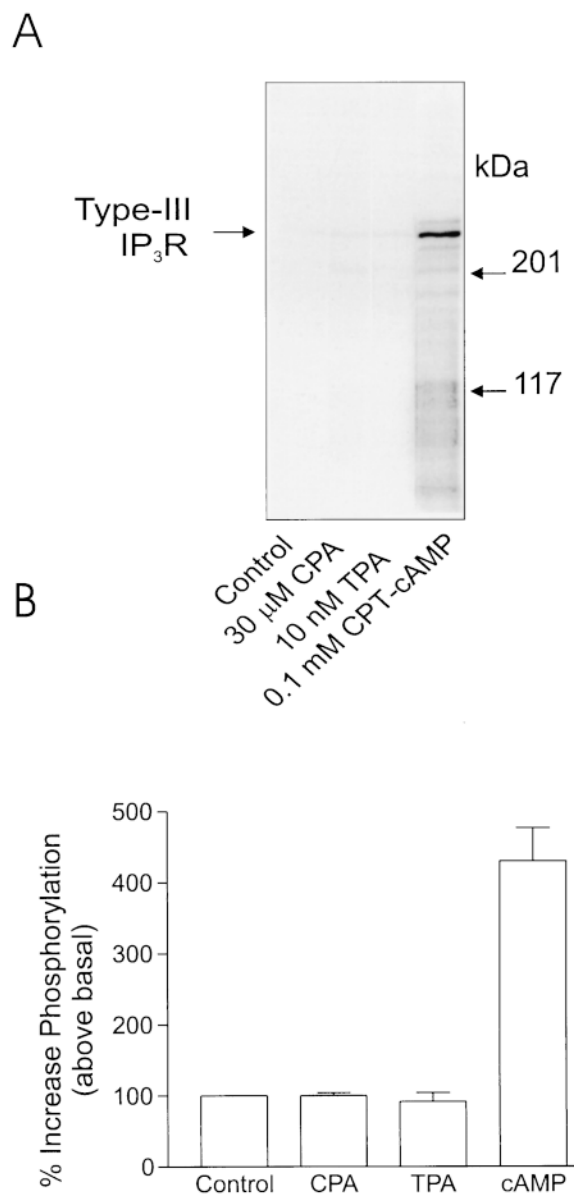
#### Model Construction

Previous mathematical models of the IP<sub>3</sub>R have tended to treat IP<sub>3</sub> as a permissive factor; its binding is re-



**Figure 2.** Phosphorylation of type-III IP<sub>3</sub> receptor after stimulation by carbachol in rat pancreatic acini. (A) Stimulation with the muscarinic agonist carbachol also results in increased phosphorylation of the type-III IP<sub>3</sub> receptor. Increased phosphorylation of the 300-kD protein could be detected at 1 μM, concentrations of carbachol that induce “peak-and-plateau” type Ca<sup>2+</sup> responses. No phosphorylation could be detected at concentrations of CCh that induce [Ca<sup>2+</sup>]<sub>i</sub> oscillations. (B) Pooled data (mean ± SEM) from at least three independent experiments, where samples were run in duplicate.

garded as obligatory for channel activation, but beyond that it has a passive role, with [Ca<sup>2+</sup>]<sub>i</sub> providing the dynamics underlying oscillations. However, two lines of experimental evidence suggest that IP<sub>3</sub> binding may play a more important, dynamic role. Firstly, binding studies have shown the affinity of IP<sub>3</sub> for its receptor is dependent on the [Ca<sup>2+</sup>]<sub>i</sub>. For type-I receptors, increasing [Ca<sup>2+</sup>]<sub>i</sub> causes either a decrease in IP<sub>3</sub>-binding affinity (Yoneshima et al., 1997) or a biphasic effect (Sienaert et al., 1997), whereas, for the type-III receptor, increasing [Ca<sup>2+</sup>]<sub>i</sub> enhances IP<sub>3</sub> binding (Yoneshima et al., 1997). Secondly, there is evidence that IP<sub>3</sub> itself may in-



**Figure 3.** Phosphorylation of type-III IP<sub>3</sub> receptor in rat pancreatic acini after stimulation by agents that modulate second-messenger levels. (A) Increased phosphorylation of the IP<sub>3</sub> receptor could be detected from acini samples incubated with CPT-cAMP, a cell-permeable cAMP analogue, but not from samples incubated with agents known to increase [Ca<sup>2+</sup>]<sub>i</sub> (30 μM CPA) or activate protein kinase C (10 nM TPA). (B) Pooled data (mean ± SEM) from at least three independent experiments, where samples were run in duplicate.

activate the IP<sub>3</sub>R. For example, experiments with high kinetic resolution performed under Ca<sup>2+</sup>-clamp conditions have shown that during continuous perfusion with a particular medium-Ca<sup>2+</sup> concentration, the introduction of IP<sub>3</sub> causes a transient release of <sup>45</sup>Ca<sup>2+</sup> from microsomes derived from rat brain synaptosomes (Finch et al., 1991) or rat hepatocytes (Dufour et al.,

1997; Marchant and Taylor, 1998). This suggests either that  $\text{IP}_3$  can inactivate the receptor or that at least some of the  $\text{Ca}^{2+}$ -induced inactivation occurs only during permeation of the channel. The  $\text{Mn}^{2+}$  quench experiments of Hajnóczky et al. (1993) demonstrate that  $\text{IP}_3$  can inactivate the receptors without permeation of  $\text{Ca}^{2+}$ . Furthermore, they found that  $\text{Ca}^{2+}$  enhanced  $\text{IP}_3$ -induced channel inactivation.

**Reaction scheme.** We assume that the complete  $\text{IP}_3\text{R}$  is composed of four, functionally identical, independent subunits. The reaction scheme governing transitions of each subunit is shown in Fig. 4.  $S$  denotes the fraction of subunits in the shut state ( $S$ ), in which the receptor channel is closed and  $\text{IP}_3$  is not bound. Binding of  $\text{IP}_3$  causes the receptor to be converted to the open state,  $O$ , and we let  $O$  (Fig. 5) denote the fraction of receptors in state  $O$ . Although several subconductance states of  $\text{IP}_3\text{R}$  have been observed, the channels most often open to just one of these (Watrás et al., 1991). We therefore assume that  $\text{IP}_3$  must be bound to all four subunits for the receptor to be in the conducting state. Thus, the fraction of conducting receptors is  $O^4$ .

To explain the apparent  $\text{IP}_3$ -induced inactivation (described above), we propose that the  $O$  state is relatively unstable, and the subunits will progress through to the more stable  $I_1$  (inactivated) state, in which  $\text{IP}_3$  is still bound but the channels do not conduct. Thus, binding of  $\text{IP}_3$  to a single binding site accounts for both channel activation and at least one aspect of inactivation. We assume that the reverse transition ( $I_1 \rightarrow O$ ) has a very slow rate, and so exclude it from our reaction scheme. It is reasonable to consider that a direct transition from  $S$  to  $I_1$  could occur. However, we suggest that the  $S \rightarrow O$  transition is greatly favored, and will therefore strongly

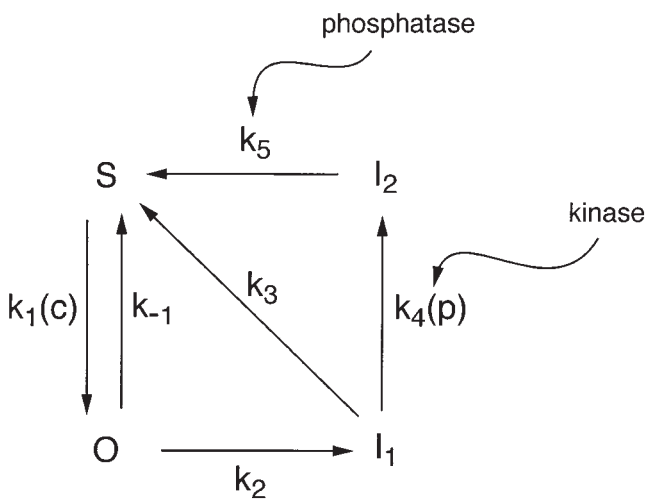


Figure 4. Diagram of the receptor states of the model of the  $\text{IP}_3$  receptor. Phosphorylation of the receptor by PKA shunts the receptor through the  $I_2$  state, thus shutting off the  $\text{Ca}^{2+}$  current, and leading to long-period oscillations.

dominate the  $S \rightarrow I_1$  transition, and so we make the simplifying assumption of setting the rate of the latter transition to zero.

In our model, we do not specifically include any binding sites for  $\text{Ca}^{2+}$ . Although it appears there may be several of these on the  $\text{IP}_3\text{R}$  (Sienaert et al., 1997), these have not been well characterized. Because of this, we instead incorporate the effects of  $\text{Ca}^{2+}$  by making the rate of the  $S$  to  $O$  transition a function of  $[\text{Ca}^{2+}]_i$ . By doing this, we are able to correlate model behavior with experimentally observed effects of  $[\text{Ca}^{2+}]_i$ , without having to speculate on the number or nature of  $\text{Ca}^{2+}$  binding sites on the receptors. This approach has the added advantage that the reaction scheme is kept simpler. However, a more complex model that assumes that  $\text{Ca}^{2+}$  governs the interconversion of the receptor between two different states, one with a high  $\text{IP}_3$  affinity, the other with a low  $\text{IP}_3$  affinity (Cardy et al., 1997; Hajnóczky and Thomas, 1997), behaves in exactly the same manner (Sneyd, LeBeau, and Yule, manuscript submitted for publication). In fact, it can be shown that, if it is assumed that  $\text{Ca}^{2+}$  binding is fast, the model presented here can be derived from this more complex model.

We set the transition  $S \rightarrow O$  to be an increasing function of  $[\text{Ca}^{2+}]_i$ . This is based on two separate experimental observations. First, raising  $[\text{Ca}^{2+}]$  increased the rate of  $^{45}\text{Ca}^{2+}$  flux in superfusion experiments (Dufour et al., 1997, data reproduced here in Fig. 5). Second, in permeabilized hepatocytes, raising the medium  $[\text{Ca}^{2+}]$  reduced the  $\text{EC}_{50}$  for  $\text{IP}_3$ -induced  $^{45}\text{Ca}^{2+}$  release from internal stores (Marshall and Taylor, 1993). Both of these experimental observations are consistent with  $\text{Ca}^{2+}$  enhancing the affinity of  $\text{IP}_3$  for the receptors. More than 80% of hepatocyte  $\text{IP}_3\text{R}$  are type II, with the remainder being type I (Wojcikiewicz, 1995), suggesting that  $\text{IP}_3$  binding to type-II receptors is enhanced by increasing  $[\text{Ca}^{2+}]$ , similar to type-III receptors (Yonishima et al., 1997). The pancreas (most of which is exocrine acinar cells) contains mostly type-III receptors, with a significant number of type-II receptors, but few type-I receptors (Wojcikiewicz, 1995). Thus, we have assumed that  $\text{Ca}^{2+}$  enhances  $\text{IP}_3$  binding to the receptors in the model.

The transition  $I_1 \rightarrow S$  represents the normal pathway by which the  $\text{IP}_3\text{R}$  recovers from inactivation, with  $\text{IP}_3$  dissociating from its binding site. The receptor can then rebind  $\text{IP}_3$  and repeat the cycle. We refer to this pathway (involving  $S$ ,  $O$ , and  $I_1$  only) as the “intrinsic” receptor pathway, on the basis that this reflects the direct effects of  $\text{IP}_3$  and  $\text{Ca}^{2+}$  on receptor activity. However, we also include a transition from  $I_1$  to  $I_2$ , where  $I_2$  represents a second inactivated state of the receptor in which  $\text{IP}_3$  is no longer bound (i.e.,  $\text{IP}_3$  dissociates during this transition). This pathway is agonist specific and involves phosphorylation of the  $\text{IP}_3\text{R}$ . As shown above,

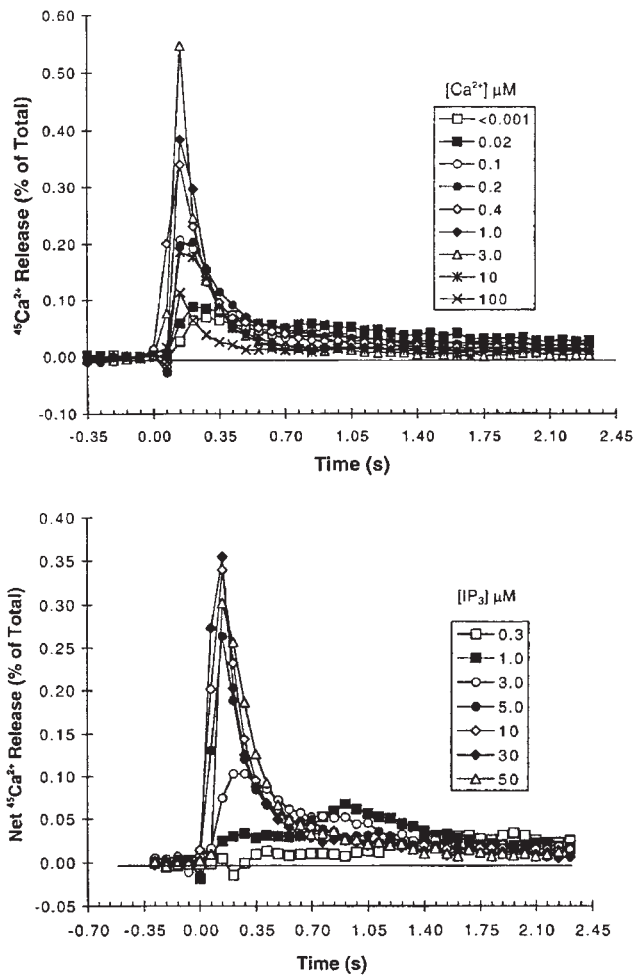


Figure 5. Data, reproduced from Dufour et al. (1997), Figures 1 A and 2 A, showing the effects of  $\text{Ca}^{2+}$  and  $\text{IP}_3$  on  $\text{Ca}^{2+}$  efflux through  $\text{IP}_3$  receptors from the rat liver. For the  $\text{Ca}^{2+}$  dose response, the concentration of  $\text{IP}_3$  was held at  $10 \mu\text{M}$  and  $[\text{Ca}^{2+}]$  was stepped up and held at the indicated concentration. For the  $\text{IP}_3$  dose response,  $[\text{Ca}^{2+}]$  was held fixed at  $400 \text{ nM}$  and  $[\text{IP}_3]$  was stepped up and held fixed at the indicated concentrations. The efflux through the receptor was then measured every 70 ms. Figure reprinted with permission.

physiological concentrations of CCK cause rapid phosphorylation of the  $\text{IP}_3\text{R}$ , (possibly via the activation of PKA), while physiological concentrations of ACh do not. Hence, to model the application of CCK,  $k_4$  is set to be nonzero, while the application of ACh is modeled by setting  $k_4 = 0$ . Phosphatase actions eventually dephosphorylate the receptor, converting it to the S state, whereupon it may rebind  $\text{IP}_3$ . A crucial element of this scheme is that while in the  $\text{I}_2$  state the receptor is unaffected by either the  $\text{IP}_3$  or  $\text{Ca}^{2+}$  concentrations. We refer to the pathway involving all four states of the channel as the “full” pathway, with the inclusion of the generation of  $\text{I}_2$  representing a “mediated” effect, as distinct from the intrinsic effects described above. The

distinction between intrinsic and mediated effects is largely for descriptive convenience.

**Receptor kinetics.** By the law of mass action differential equations for the various receptor states can be determined. The equation for the fraction of receptor subunits in the open state ( $O$ ) is

$$\frac{dO}{dt} = k_1 p S - k_{-1} O - k_2 O, \quad (1)$$

where  $p$  is  $[\text{IP}_3]$ . The variable  $S$  can be eliminated using the conservation law  $S = 1 - (O + \text{I}_1 + \text{I}_2)$ . Here,  $\text{I}_1$  and  $\text{I}_2$  are the fraction of receptors in states  $\text{I}_1$  and  $\text{I}_2$ , respectively. As previously stated, we assume that all four of the subunits must be in this state before the receptor will pass any  $\text{Ca}^{2+}$  current. Thus the conducting state is  $O^4$ .

The equation for  $\text{I}_1$  is given by

$$\frac{d\text{I}_1}{dt} = k_2 O - (k_3 + k_4) \text{I}_1, \quad (2)$$

and for  $\text{I}_2$  by

$$\frac{d\text{I}_2}{dt} = k_4 \text{I}_1 - k_5 \text{I}_2. \quad (3)$$

As described above, the rate  $k_1$  is a function of  $[\text{Ca}^{2+}]_i$ , which is denoted by  $c$ :

$$k_1 = \frac{\alpha_1 c^3}{\beta_1^3 + c^3}, \quad (4)$$

whereas  $k_{-1}$ ,  $k_2$ ,  $k_3$ , and  $k_5$  are constants. The constant  $\alpha_1$  is the maximum rate of the S to O transition, and  $\beta_1$  is the  $\text{Ca}^{2+}$  concentration at which the rate of the S to O transition is half its maximum rate. The function  $k_1$  is an increasing function of  $c$ , representing our assumption that  $[\text{Ca}^{2+}]_i$  enhances the affinity of  $\text{IP}_3$  binding. Little is known regarding the mechanism(s) by which  $\text{Ca}^{2+}$  exerts its effects on the  $\text{IP}_3\text{R}$ , and therefore, although  $\text{Ca}^{2+}$  may act by directly binding to the receptor, our reaction scheme does not explicitly indicate such a mechanism. However, as discussed above, the present model can be derived from a more general model in which  $\text{Ca}^{2+}$  regulates the binding affinity of  $\text{IP}_3$  (Hajnóczky and Thomas, 1997; Cardy et al., 1997; Sneyd, LeBeau, and Yule, manuscript submitted for publication).

Since we have not suggested explicit mechanisms representing the transitions governed by  $k_1$ ,  $k_2$ , and  $k_3$ , we use the simplest possible functions. Thus, we chose  $k_2$  and  $k_3$  as constants, and let  $k_1$  be a sigmoidal function of  $c$ , with a Hill coefficient of 3. If  $k_1$  is assumed to have a smaller Hill coefficient, it is more difficult to get oscillations in the model. It thus appears that cooperativity in the action of  $\text{Ca}^{2+}$  on  $\text{IP}_3$  binding may be an important physiological mechanism. These choices for the rate constants are easily modified to give bell-shaped steady state open probability curves if one wishes to

model other types of IP<sub>3</sub> receptors. For instance, with a bell-shaped open probability curve, oscillations occur in the model even when  $k_1$  has a Hill coefficient of 1 (computations not shown).

The rate constant  $k_4$  is given by

$$k_4 = \frac{\alpha_4 p}{\beta_4 + p}, \quad (5)$$

and models the action of a kinase (possibly PKA) on the IP<sub>3</sub>R, and is assumed to be dependent on the type of agonist used to initiate Ca<sup>2+</sup> oscillations. The constant  $\alpha_4$  denotes the maximum rate of the reaction attained at high  $p$ , while  $\beta_4$  denotes the value of  $p$  at which the rate is half maximal. When activated,  $k_4$  shunts the receptors through the I<sub>2</sub> pathway. Since it is reasonable to assume that greater levels of agonist stimulation will result in greater kinase activity, we assume that  $k_4$  is a saturating function of the IP<sub>3</sub> concentration. As can be seen from Table I,  $\beta_4$  is chosen to be relatively small, so that the rate of phosphorylation saturates quickly, and, in most physiological regimes, is approximately constant.

**Simulation of IP<sub>3</sub>- and Ca<sup>2+</sup>-clamp experiments.** To determine reasonable values for the transition rates, we simulated experiments in which a superfusion system was used to determine the rapid kinetics of IP<sub>3</sub>R activation and inactivation. This technique has the feature that extravesicular [IP<sub>3</sub>] and [Ca<sup>2+</sup>] can be rapidly changed under otherwise clamped conditions (Finch et al., 1991; Dufour et al., 1997; Marchant and Taylor, 1998). Unfortunately, such data are not available from type-III receptors, and so it is unknown whether their time-dependent behavior is similar to that of type-I or -II receptors. In the absence of evidence to the contrary, we shall assume it is, although the model does point out some likely important differences, as we shall see.

The experimental observations we are attempting to reproduce are shown in Fig. 5, A and B. Fig. 5 A depicts

<sup>45</sup>Ca<sup>2+</sup> efflux for various extravesicular [Ca<sup>2+</sup>], with a constant [IP<sub>3</sub>] of 10 μM. Initially, increasing the bathing [Ca<sup>2+</sup>] increased both the initial rate and peak response of <sup>45</sup>Ca<sup>2+</sup> efflux, but these factors decreased at high [Ca<sup>2+</sup>]. The cumulative release was also found to increase initially, but then decrease at higher [Ca<sup>2+</sup>] (Dufour et al., 1997, not shown). Fig. 5 B shows the results of similar experiments in which extravesicular [IP<sub>3</sub>] was changed, while the [Ca<sup>2+</sup>] was fixed at 400 nM. Here, again, increasing [IP<sub>3</sub>] caused an increase in both the initial rate and cumulative <sup>45</sup>Ca<sup>2+</sup> release, although in this case neither factor was observed to decline at high [IP<sub>3</sub>] (Dufour et al., 1997).

Simulations of these experiments are shown in Fig. 6. Since only direct effects of IP<sub>3</sub> and Ca<sup>2+</sup> would be expected to affect IP<sub>3</sub>R activity, only the intrinsic pathway was used for these simulations (i.e., generation of I<sub>2</sub> was excluded by setting  $k_4 = 0$ ). The simulated experiments used the same concentrations of agonists, although the full range was not used. The qualitative behavior of the simulations was in good agreement with the experimental data, with one significant difference. The rate of inactivation of the receptor is an increasing function of [Ca<sup>2+</sup>]<sub>i</sub> in the data but not in the model. In other words, the data from type-II receptors indicates that  $k_2$  is an increasing function of  $c$ , but this was not included in the model. The principal reason for this is that we

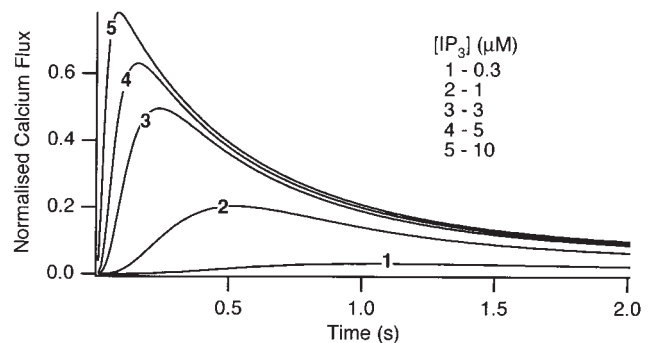
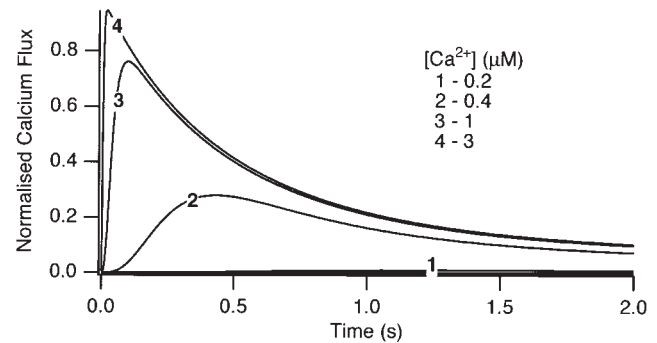


Figure 6. Dose responses, calculated from the model. The same Ca<sup>2+</sup> and IP<sub>3</sub> concentrations as in Fig. 5 were used, except that the whole range of concentrations was not covered.

table i

Parameter Values for the IP<sub>3</sub>R Model

Parameter	Description	Value
$k_{flux}$	Maximum IP <sub>3</sub> R flux rate	28 μM · s <sup>-1</sup>
$J_{influx}$	Ca <sup>2+</sup> leak rate	0.4 (0.025) μM · s <sup>-1</sup>
$V_p$	Maximum pump rate	2.6 (0.2) μM · s <sup>-1</sup>
$K_p$	[Ca <sup>2+</sup> ] <sub>i</sub> for half-maximal pumping	0.54 μM
$\alpha_1$	Maximum rate of $k_1$	40 μM · s <sup>-1</sup>
$\beta_1$	[Ca <sup>2+</sup> ] <sub>i</sub> for half-maximal $k_1$	0.8 μM
$k_{-1}$	Rate of O to S transition	0.88 s <sup>-1</sup>
$k_2$	Rate of O to I <sub>1</sub> transition	0.5 s <sup>-1</sup>
$k_3$	Rate of I <sub>1</sub> to S transition	0.5 s <sup>-1</sup>
$\alpha_4$	Maximum rate of $k_4$	0 (0.06) s <sup>-1</sup>
$\beta_4$	[IP <sub>3</sub> ] for half-maximal $k_4$	0.01 μM
$k_5$	Rate of I <sub>2</sub> to S transition	0.02 s <sup>-1</sup>

The values in brackets are those used to model CCK-induced oscillations.



found, in order to obtain a monotonic steady state open probability curve (see below), it was simplest to set  $k_2$  to be a constant, rather than an increasing function of  $c$ . Although the dynamic properties of type-III IP<sub>3</sub> receptors have not yet been measured, our model predicts that a monotonic steady state curve will likely be associated with receptors whose rate of inactivation is independent of  $[Ca^{2+}]_i$ . The simulated dose responses of the model also agree qualitatively with the results of Marchant and Taylor (1998).

**Monotonic steady state  $[Ca^{2+}]$  dependence.** For type-I IP<sub>3</sub> receptors, the steady state open probability has been found to have a bell-shaped dependence on  $[Ca^{2+}]$  (Bezprozvanny and Ehrlich, 1995; Taylor and Traynor, 1995; Kaftan et al., 1997), and this can easily be reproduced by our model (computations not shown). However, recent results (Hagar et al., 1998) have shown that the type-III IP<sub>3</sub>R has a steady state open probability curve that is a monotonic increasing function of  $Ca^{2+}$ . Since it appears that  $Ca^{2+}$  oscillations in pancreatic acinar cells are governed by  $Ca^{2+}$  release through type-III IP<sub>3</sub>R, we chose parameter values so as to obtain a monotonically increasing steady state open probability curve as a function of  $Ca^{2+}$  concentration (Fig. 7).

Fig. 7 shows that as  $[IP_3]$  is increased, the point of inflexion (i.e., where the slope is greatest) shifts to the left. Since the measurement of the steady state open probability curve has been measured at only a single IP<sub>3</sub> concentration, this is a prediction from our model that has not yet been tested.

In the APPENDIX, we show that, at least in most current models, including those of Tang et al. (1996), De Young and Keizer (1992), Atri et al. (1993), Bezprozvanny (1994), and Li and Rinzel (1994), the position of the steady state open probability curve as a function of IP<sub>3</sub> concentration is crucially dependent on the as-

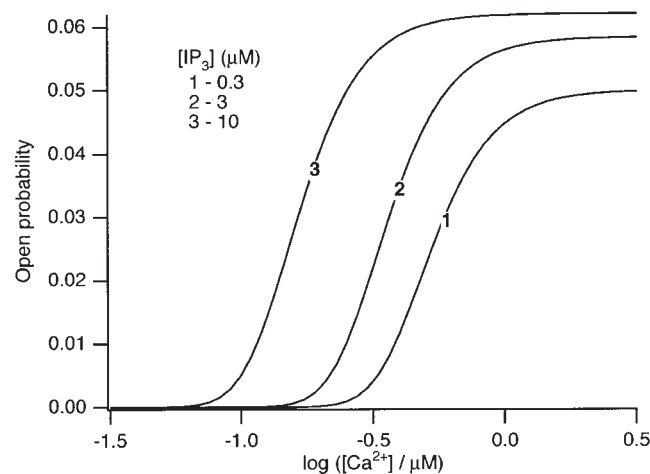


Figure 7. Steady state open probability of the model IP<sub>3</sub> receptor, as a function of  $[Ca^{2+}]_i$ , for a range of constant IP<sub>3</sub> concentrations.

sumed effects of  $Ca^{2+}$  on IP<sub>3</sub> binding. When an increased  $Ca^{2+}$  concentration enhances IP<sub>3</sub> binding to the receptor, the models predict that the steady state curve will move to the left as the background  $[IP_3]$  increases. Conversely, when an increased  $Ca^{2+}$  concentration decreases IP<sub>3</sub> binding to the receptor, the steady state curve is predicted to move to the right as  $[IP_3]$  increases.

The rightward shift of the peak of the bell-shaped steady state curve observed by Kaftan et al. (1997) came from studies of the type-I IP<sub>3</sub>R. Binding of IP<sub>3</sub> to the type-I receptor is decreased by raising  $[Ca^{2+}]$  (Yoneshima et al., 1997; but see Sienaert et al., 1997 for more complex effects), whereas IP<sub>3</sub> binding to type-III receptors was enhanced by raising  $[Ca^{2+}]$  (Yoneshima et al., 1997). Thus, from analysis of our model, the rightward shift of the steady state curve observed by Kaftan et al. (1997) is the expected effect for type-I receptors, but the opposite should occur in cases where  $Ca^{2+}$  enhances IP<sub>3</sub> binding, which appears to be the appropriate situation for pancreatic acinar cells.

We emphasise another crucial point that is often overlooked. The exact nature of the steady state open probability curve has little effect on the dynamic properties of the receptor, and thus has little influence on whether or not the receptor is able to mediate  $Ca^{2+}$  oscillations. This is because it is the initial fast activation of the IP<sub>3</sub>R, followed by a slower inactivation, that is the crucial mechanism underlying  $Ca^{2+}$  oscillations. As we shall see, a model with a monotonic steady state curve is quite capable of generating oscillations, and in fact these oscillations are almost the same as those of a similar model in which the steady state open probability curve is bell shaped (computations not shown).

**Incorporation into a whole-cell model.** We now incorporate the receptor model into a description of acinar cell  $[Ca^{2+}]_i$  responses, endeavoring to keep the model as simple as is reasonably possible so as to retain the focus on the kinetics of the IP<sub>3</sub>R. Hence, we do not include any possible effects of ryanodine receptors (see DISCUSSION).

The equation for  $[Ca^{2+}]_i$  ( $c$ ) is given by

$$\frac{dc}{dt} = J_{rel} - J_{pump} + J_{influx}, \quad (6)$$

where  $J_{rel}$  represents the IP<sub>3</sub>-induced release of  $Ca^{2+}$  from the ER and is given by

$$J_{rel} = k_{flux} O^4, \quad (7)$$

in which  $k_{flux}$  is the maximum rate of  $Ca^{2+}$  release from the ER.

$J_{pump}$  represents the combined activity of all  $Ca^{2+}$  pumps that remove  $Ca^{2+}$  from the cytosol and is given by

$$J_{pump} = \frac{V_p c^2}{K_p^2 + c^2}, \quad (8)$$

where  $V_p$  represents the maximum rate of pumping and  $K_p$  is the  $[Ca^{2+}]_i$  for half-maximal pumping. The  $Ca^{2+}$  ATPase pump is assumed to operate in a cooperative manner, with a Hill coefficient of 2 (Lytton et al., 1992).

$J_{influx}$  is an adjustable parameter that represents a constant rate of  $Ca^{2+}$  influx into the cytosol. This term includes both influx from outside the cell and any leak of  $Ca^{2+}$  from intracellular stores such as the ER and mitochondria.

The standard parameter values are given in Table I. The values in brackets correspond to those values used to model CCK-induced oscillations, as described in more detail below.

To keep the model as simple as possible at this stage, we do not consider effects such as spatial variation in the  $[Ca^{2+}]_i$  signals, separation of either  $Ca^{2+}$  influx versus leak from internal stores, or the various forms of  $Ca^{2+}$  pumping both into internal stores or out of the cell. We also do not consider the aspect of store filling state and the dependence on this of  $[Ca^{2+}]_i$  signals, nor do we include capacitative  $Ca^{2+}$  entry. Thus, we are concerned only with the initial phases of the  $[Ca^{2+}]_i$  signals (i.e., the generation of the responses), when the filling state of the  $Ca^{2+}$  stores will not yet have been compromised, as opposed to the sustained phases of the responses. We leave such aspects for further investigation.

In addition to our need to keep the model as simple as possible at this stage, there is another very good reason to omit consideration of spatial effects at this stage. It is well known that, to understand the behavior of a reaction–diffusion system (such as this would be in the presence of  $Ca^{2+}$  diffusion), it is necessary first to understand the behavior of the model in the absence of diffusion; i.e., the reaction kinetics must be understood in detail before it is possible to understand how diffusion will affect the system. Although diffusion and spatial heterogeneities will modulate the amplitude and period of the oscillations, they are unlikely, by themselves, to explain the gross features of the different oscillation types. Only a study of the reaction mechanisms will do that.

Finally, we assume that  $Ca^{2+}$  buffering is fast and linear, so that all the fluxes in the model are effective fluxes of free  $Ca^{2+}$ . In the absence of any specific information on the properties of calcium buffers in pancreatic acinar cells, this is the simplest assumption.

### Theoretical Results

**Parameter values.** The parameter values used in the model simulations are presented in Table I. The values for the rates of activation and inactivation of the  $IP_3$  receptor by  $Ca^{2+}$  ( $\alpha_1$ ,  $\beta_1$ ,  $\alpha_2$ ,  $\beta_2$ ,  $\gamma_2$ ,  $\alpha_3$ ,  $\beta_3$ ,  $k_{-1}$ , and  $k_2$ ) were determined by ensuring the model agrees with the results of Dufour et al. (1997). This was not done by

a detailed fitting procedure, only approximate agreement was required. The parameters governing the rate of phosphorylation of the  $IP_3$  receptor by PKA ( $\alpha_4$  and  $\beta_4$ ), and the recovery from the  $I_2$  state ( $k_5$ ), were not determined from experimental data; the values in Table I were chosen so as to give reasonable agreement with the observed CCK-induced oscillations. For ACh-induced oscillations,  $\alpha_4$  was set to zero to mimic the much decreased rate of receptor phosphorylation.

**Pumping rates.** To measure the approximate rate of  $Ca^{2+}$  ATPase activity, exponential functions were fit to the downward slopes of the oscillations induced by either ACh or CCK (data not shown). Although this assumes that the decline in  $Ca^{2+}$  concentration during the decreasing phase of the oscillation is due to  $Ca^{2+}$  pumping, and although it assumes the pumping has linear kinetics, these assumptions will have little, if any, qualitative effect on the result, and are accurate enough for our purposes; we are not doing a detailed fit of the model to data, merely using the data to determine approximate values for the parameters.

ACh-induced oscillations have a declining phase that approximates an exponential curve, with a decay rate that varies from  $\sim 0.2$  to  $\sim 0.4$   $s^{-1}$ . On the other hand, the decay rate for the decreasing phase of CCK-induced oscillations ranges from  $\sim 0.03$  to  $\sim 0.06$   $s^{-1}$ .

Based on these experimentally measured time constants for the removal of  $Ca^{2+}$  from the cytoplasm, we chose two different values for  $V_p$ , the maximum pumping rate, corresponding to the two different agonists. For ACh, we chose  $V_p = 2.6$   $\mu M s^{-1}$ , while for CCK we chose  $V_p = 0.2$   $\mu M s^{-1}$  (Table I). Note that, although  $V_p$  does not correspond directly to the time constants measured by fitting an exponential to the experimental data, these maximum pumping rates will give rates of decline of the correct orders of magnitude for the two different agonists. Based on the data of Lytton et al. (1992), the pump was assumed to operate in a cooperative fashion, with a half-maximal rate occurring at 0.54  $\mu M$ . The parameter  $k_{influx}$  was determined by requiring a physiologically reasonable resting  $Ca^{2+}$  concentration.

**Calcium influx.** There remains only one parameter, the rate of  $Ca^{2+}$  influx, to discuss. We hypothesize that this parameter is agonist dependent. In addition to the very different kinetics of  $[Ca^{2+}]_i$  transients evoked by the two agonists, the transients also differ greatly in their sensitivity to removal of external  $Ca^{2+}$ . ACh-induced transients are very sensitive, such that if the medium bathing cells is switched from normal (1.2 mM  $[Ca^{2+}]$ ) to nominally  $Ca^{2+}$ -free during repetitive  $[Ca^{2+}]_i$  oscillations, the oscillations are abolished within  $\sim 30$  s (Yule et al. 1991). This behavior has also been observed by Muallem et al. (1990), and for bombesin-stimulated oscillations in rat pancreatic acinar cells by Xu et al. (1997).

The same treatment has only a slow effect on CCK-induced oscillations (Yule et al. 1991; see also Xu et al., 1997). Here, the oscillations may continue for up to 20 min, with the peak of the transients slowly reducing. The slow decay, and eventual loss, of CCK-induced oscillations probably reflects  $\text{Ca}^{2+}$  store depletion, which is normally prevented, when  $\text{Ca}^{2+}$  is present in the medium, by capacitative  $\text{Ca}^{2+}$  entry (Xu et al., 1995, 1997), which is not included in the model at this stage. It seems unlikely that the same explanation can account for the effects of removal of external  $\text{Ca}^{2+}$  on ACh-induced oscillations because of the contrasting rapidity of the loss of oscillations. Instead, the experimental observations suggest that ACh may activate a  $\text{Ca}^{2+}$  entry pathway that is necessary for the generation of oscillations. This is consistent with the raised baseline  $\text{Ca}^{2+}$  concentrations observed during ACh-induced oscillations. Although it is clear that the mechanisms of  $\text{Ca}^{2+}$  entry are much more complicated than our model assumes (Loessberg et al., 1991; Xu et al., 1995, 1997), we ignore these complications for now and just treat  $\text{Ca}^{2+}$  influx as a simple leak. It is unclear what qualitative effect this will have on the model conclusions.

Based on the above argument, we assume that ACh increases the rate of  $\text{Ca}^{2+}$  influx from outside the cell, while CCK does so to a much lesser extent, and thus, to simulate the two different types of oscillations, we use the two different values shown in Table I.

It is important to note that only three parameters are dependent on the agonist. All other parameters are invariant for all the simulations. Thus, we hypothesise that the differences between oscillations induced by ACh, and those induced by CCK, are due to the following two things. (a) CCK activates PKA, and causes greater phosphorylation of the  $\text{IP}_3$  receptor, thus shunting it through the closed state  $I_2$ . ACh-induced phosphorylation is much less significant, and thus the state  $I_2$  is bypassed. (b) ACh increases the rate of  $\text{Ca}^{2+}$  turnover much more than CCK does. Thus, the rate of  $\text{Ca}^{2+}$

influx from outside the cell, and the rate of  $\text{Ca}^{2+}$  removal from the cytoplasm, are greater in the presence of ACh than in the presence of CCK.

**ACh-induced oscillations.** We investigated the effects of increasing  $[\text{IP}_3]$  on  $[\text{Ca}^{2+}]_i$  responses in the model, with the pathway regulated by  $k_4$  switched off. The rates of  $\text{Ca}^{2+}$  influx and pumping were set to 0.4 and 2.6  $\mu\text{M s}^{-1}$ , respectively (see Table I). Raising  $[\text{IP}_3]$  to 0.66  $\mu\text{M}$  caused the generation of  $[\text{Ca}^{2+}]_i$  oscillations with a period of  $\sim 15$  s (Fig. 8). During the oscillatory behavior, the nadir of the oscillations occurred at  $\sim 300$  nM, well above the resting  $[\text{Ca}^{2+}]_i$ .

For the simulation in Fig. 8,  $[\text{IP}_3]$  was not raised immediately to its final level, but was instead raised gradually, with a time constant of 10 s. Thus, our simulations include the effects of a continually varying  $\text{IP}_3$  concentration, as would be expected to occur upon agonist stimulation. Although slow variations in  $[\text{IP}_3]$  modulate the exact shape of the oscillations, their overall behavior can still be predicted by considering the behavior in response to a constant  $[\text{IP}_3]$ . Similarly, if  $[\text{IP}_3]$  is allowed to decrease gradually, the oscillations eventually disappear (computations not shown). The crucial point to notice is that, although  $[\text{IP}_3]$  is changing slightly throughout the course of an oscillation (particularly during the first few peaks), such changes are not a crucial part of the oscillatory mechanism. Oscillations can occur in the presence of a fixed  $[\text{IP}_3]$  in the oscillatory range.

The behavior of the system over a full range of  $[\text{IP}_3]$  can be seen in Fig. 9. In this figure, the effect of increasing  $[\text{IP}_3]$  progressively on the behavior of the system is shown. In particular, this analysis examines the effect of  $[\text{IP}_3]$  on  $[\text{Ca}^{2+}]_i$  responses, showing where they are stable and where they are oscillatory. Starting at low  $[\text{IP}_3]$  values, the system is stable, as depicted by the solid line. As  $[\text{IP}_3]$  is progressively increased,  $[\text{Ca}^{2+}]_i$  gradually rises, but it still stable (i.e., it remains at a single value over time). However, at  $[\text{IP}_3] = 0.62$ , a

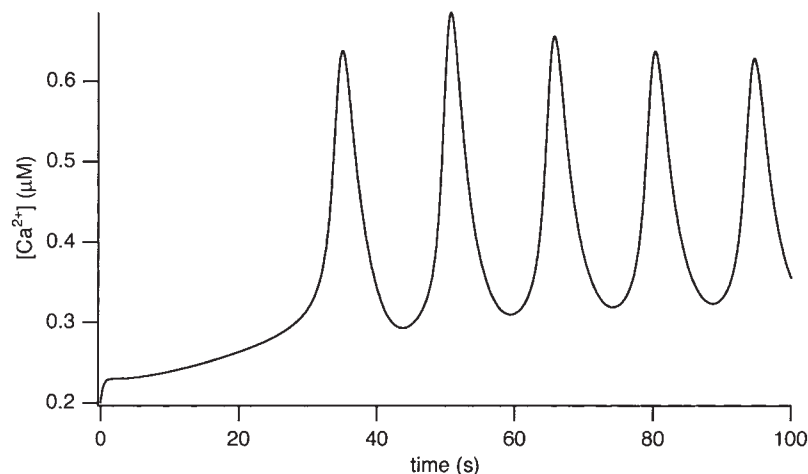


Figure 8. Typical ACh-induced oscillations in the model for  $[\text{IP}_3] = 0.66 \mu\text{M}$ .

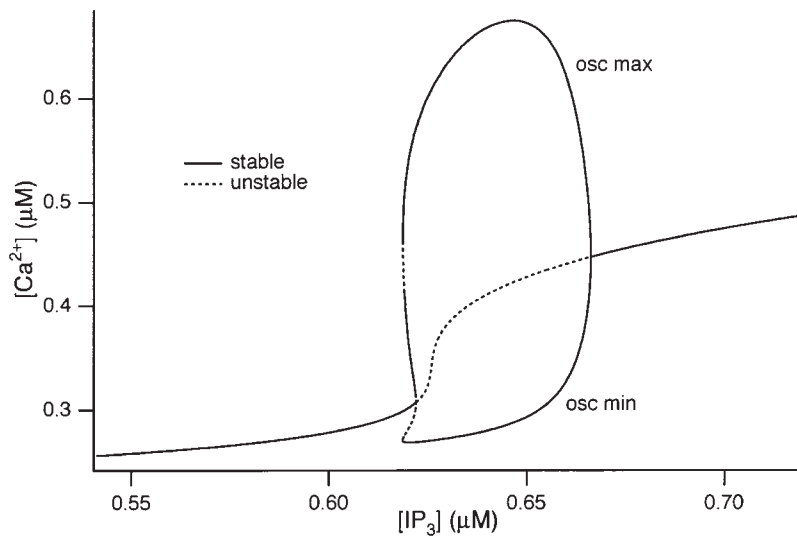


Figure 9. Bifurcation diagram for ACh-induced model oscillations showing the values of  $[IP_3]$  for which oscillations occur. A dotted line denotes an unstable steady state, while a solid line denotes a stable steady state or a stable oscillation.

critical point is reached where the steady state solution becomes unstable (Fig. 9, dotted line) and a stable periodic solution (i.e., oscillations) emerges. The maximum and minimum amplitudes of the periodic solution are depicted by the solid lines. This “oscillatory regime” reflects values of  $[IP_3]$  at which steady oscillations of  $[Ca^{2+}]_i$  are observed. When  $[IP_3]$  exceeds 0.67, the periodic solution collapses back to a stable, steady state value that is raised considerably compared with that at  $[IP_3]$  before the periodic region.

From Fig. 9, two other important features are apparent. The first is that, at  $[IP_3]$  just before the oscillatory regime,  $[Ca^{2+}]_i$  is raised relative to the resting level and, for  $[IP_3]$  values that give oscillations, the minimum value of  $[Ca^{2+}]_i$  during the oscillations also remains elevated compared with the resting  $[Ca^{2+}]_i$ . This feature therefore corresponds to the raised baseline  $[Ca^{2+}]_i$  during oscillations that are observed in both the experimental and simulated oscillations (Yule et al. 1991; and Fig. 8).

The second feature from Fig. 9 is that the range of  $[IP_3]$  over which oscillations are generated is very narrow ( $\approx 50$  nM). This feature is consistent with the experimental observation that only a narrow range of ACh concentrations is able to elicit oscillations of  $[Ca^{2+}]_i$  (Yule and Gallacher, 1988). It seems reasonable to assume that the narrow range of ACh concentrations generates a relatively narrow range of  $[IP_3]$ , although assays for  $IP_3$  are not yet sensitive enough to test this prediction.

**CCK-induced  $[Ca^{2+}]_i$  oscillations.** The experimental results indicate that CCK (but not ACh) activates PKA, which phosphorylates the inactivated ( $I_1$  state) receptors, converting them to the  $I_2$  state. The receptors remain in the  $I_2$  state, where they are insensitive to  $[Ca^{2+}]_i$ , until the action of phosphatases converts them back to the S state. The action of PKA was modeled by

increasing  $k_4$  to  $0.05$  s $^{-1}$ . Furthermore, we reduced the rate of  $Ca^{2+}$  turnover by decreasing  $V_p$ , the maximum pump rate, to  $0.2$   $\mu\text{M s}^{-1}$ , while the rate of  $Ca^{2+}$  influx was reduced to  $0.025$   $\mu\text{M s}^{-1}$ .

Simulated CCK-induced  $[Ca^{2+}]_i$  oscillations are shown in Fig. 10. At  $0.6$   $\mu\text{M}$   $[IP_3]$ , after a large initial spike, repetitive  $[Ca^{2+}]_i$  transients occur with a period of  $\sim 150$  s. The  $[Ca^{2+}]_i$  spike kinetics are consistent with the experimental data and the spikes originate from close to the basal  $[Ca^{2+}]_i$ , in contrast to the ACh-induced oscillations. Again, for this simulation,  $[IP_3]$  was raised gradually with a time constant of 100 s to mimic more realistically the effects of agonist application.

The bifurcation diagram for the full (CCK-activated) model is shown in Fig. 11. The threshold  $[IP_3]$  for generating oscillations occurs at  $\sim 0.56$   $\mu\text{M}$ , at which large oscillations occur. Before this, raising  $[IP_3]$  causes little increase in  $[Ca^{2+}]_i$ . As  $[IP_3]$  is increased through the oscillatory regime, the nadir of the periodic solution (i.e., the minimum  $[Ca^{2+}]_i$  value during repetitive oscillations) remains close to the resting value, corresponding to the baseline nature of the oscillations. The minimum  $[Ca^{2+}]_i$  only starts to increase as the periodic solution collapses to the stable steady state solution at  $\sim 0.77$   $\mu\text{M}$   $[IP_3]$ . In contrast, the maximum  $[Ca^{2+}]_i$  during oscillations is large at the threshold  $[IP_3]$  and falls markedly as  $[IP_3]$  is further increased. It should be noted though, that the maximum amplitude of the initial  $[Ca^{2+}]_i$  spike will depend on the rate of  $IP_3$  accumulation and will typically overshoot the maximum value of the periodic solution.

The bifurcation diagram shows that simulated CCK-induced oscillations occur for a larger range of  $[IP_3]$  than is the case of ACh (compare Fig. 11 with 9). This is consistent with experimental observations that ACh-induced oscillations occur for only a very narrow con-

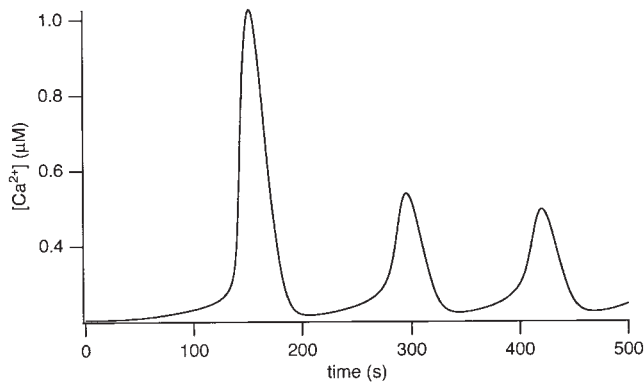
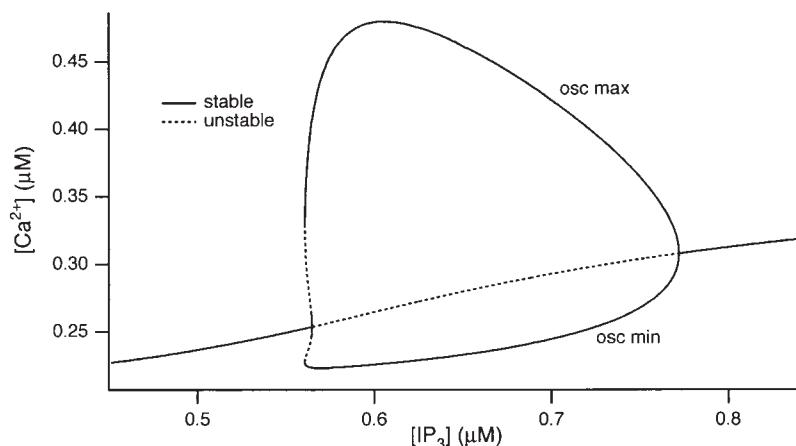


Figure 10. Typical CCK-induced oscillations in the model for  $[IP_3] = 0.6 \mu\text{M}$ .

centration range, whereas a wider range of CCK concentration is effective at generating oscillations (Yule, D.I., unpublished data). Finally, Fig. 11 shows that, for  $[IP_3]$  above  $\sim 0.77 \mu\text{M}$ , a stable steady state solution corresponding to a maintained plateau  $[Ca^{2+}]_i$  occurs.

#### Testing Model Predictions

**Experiments with  $Ca^{2+}$ -free media.** We used the model to investigate the relationship between the rate of  $Ca^{2+}$  influx and generation of ACh-induced  $[Ca^{2+}]_i$  oscillations. By reducing  $J_{\text{influx}}$ , we can simulate the effect of reducing extracellular  $[Ca^{2+}]$ . It turns out that, as  $J_{\text{influx}}$  is decreased, the range of  $IP_3$  concentrations for which oscillations are observed shifts to the right; i.e., to higher  $[IP_3]$ . Thus, a decrease in calcium influx would be expected to abolish oscillations, while an increase in  $[IP_3]$  would be expected to restore them. This behavior is demonstrated in Fig. 12 A. The values for  $J_{\text{influx}}$  and  $[IP_3]$  are indicated at the top of the figure. At the normal  $J_{\text{influx}}$  value of  $0.4 \mu\text{M s}^{-1}$ , oscillations are induced when the concentration of  $IP_3$  is raised to  $0.66 \mu\text{M}$ . Reducing  $J_{\text{influx}}$  to  $0.35 \mu\text{M s}^{-1}$  abolishes the oscillations, but these are recovered when  $[IP_3]$  is increased to  $0.75 \mu\text{M}$ .



Experiments were conducted to test these model predictions (Fig. 12 B). Acinar cells were exposed to  $70 \text{ nM}$  ACh, which evoked repetitive oscillations in the presence of  $1.2 \text{ mM}$  external  $Ca^{2+}$ . At  $t = 280 \text{ s}$ , the external  $Ca^{2+}$  concentration was reduced to  $100 \text{ mM}$ , which abolished oscillations within one to two oscillation periods. An increase in the ACh concentration (to  $100 \text{ nM}$ ) at  $350 \text{ s}$ , still in the presence of low external  $Ca^{2+}$ , restored the oscillations, this time with an increased frequency. The increased frequency is also sometimes seen in the model (computations not shown).

Comparison of Fig. 12, A and B, shows that the model predictions are confirmed by the experimental data. In the presence of CCK, removal of external  $Ca^{2+}$  has no immediate effect on the  $Ca^{2+}$  oscillations (Yule et al., 1991), and this effect is also reproduced by the model (computations not shown).

**Effects of phosphorylation on ACh-induced oscillations.** Using the model, we studied the effects of phosphorylating the  $IP_3$  receptors during ACh-induced oscillations (computations not shown). Oscillations are initiated by  $0.66 \mu\text{M}$   $IP_3$ , with the other parameters the same as for ACh-induced oscillations (Table I); in particular,  $\alpha_4 = 0$  to simulate the absence of phosphorylation. Then, at  $100 \text{ s}$ ,  $\alpha_4$  was increased to  $0.05 \text{ s}^{-1}$ , to simulate the cAMP-induced phosphorylation of the receptor by PKA. Oscillations are quickly abolished. This prediction is confirmed by existing experimental data (Camello et al., 1996) and our own experiments, in which oscillations induced by  $100 \text{ ACh}$  are quickly abolished by the addition of  $0.1 \text{ mM}$  CPT-cAMP (Yule, D.I., unpublished data).

Although phosphorylation of the receptor can lead to long-period oscillations in the absence of fast membrane transport of  $Ca^{2+}$  (recall that CCK does not increase the membrane transport of  $Ca^{2+}$  as much as ACh does), it is unable to do so in the presence of large fluxes of  $Ca^{2+}$  across the membrane. Essentially, the  $Ca^{2+}$  ATPase pumps remove  $Ca^{2+}$  so quickly from the cytoplasm that the  $Ca^{2+}$  flux through the  $IP_3R$  (which,

Figure 11. Bifurcation diagram for CCK-induced model oscillations, showing the values of  $[IP_3]$  for which oscillations occur. A dotted line denotes an unstable steady state, while a solid line denotes a stable steady state, or a stable oscillation.

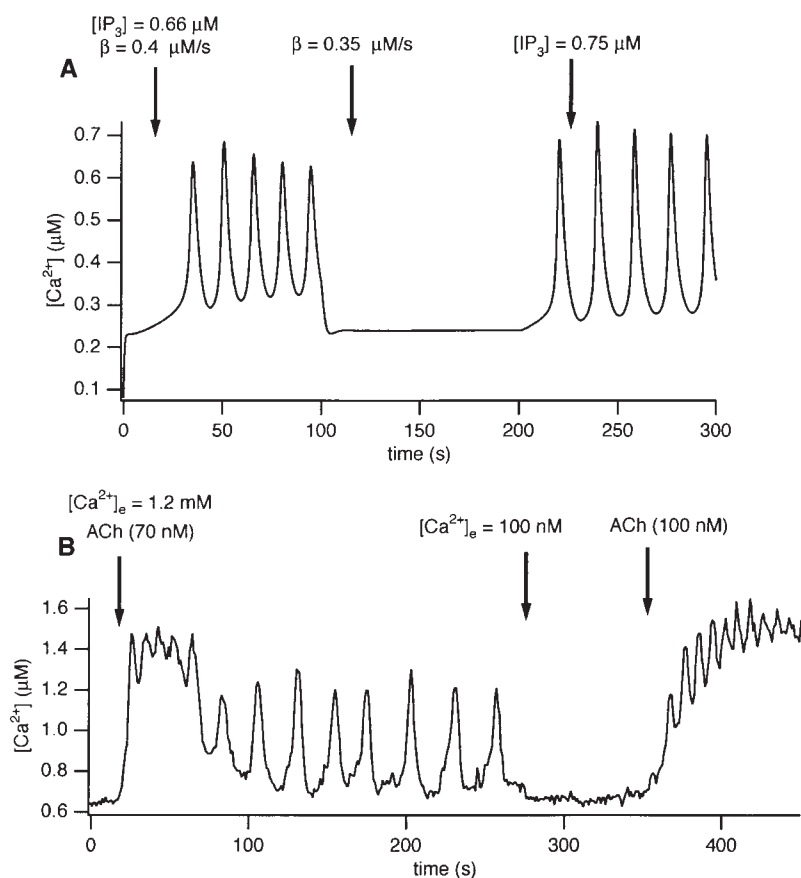


Figure 12. (A) The effect of reducing external  $\text{Ca}^{2+}$  in the model. ACh-induced oscillations are abolished by reducing to  $0.35 \mu\text{M s}^{-1}$  the  $\text{Ca}^{2+}$  influx from outside the cell. Oscillations are then restored by increasing the  $\text{IP}_3$  concentration to  $0.75 \mu\text{M}$ . (B) Experimental test of the prediction in A. Mouse pancreatic acinar cells were first exposed to  $70 \text{ nM}$  ACh in the presence of  $1.2 \text{ mM}$   $\text{Ca}^{2+}$ , which initiated oscillations. Reduction of external  $\text{Ca}^{2+}$  to  $100 \text{ nM}$  abolished the oscillations, but an increase in ACh concentration to  $100 \text{ nM}$  restored the oscillations, as predicted by the model.

it must be recalled, is now sitting in a closed phosphorylated state much of the time) cannot keep up the oscillatory cycle. It is only when the  $\text{IP}_3\text{R}$  is not shunted into the phosphorylated state that the receptor cycle is fast enough to maintain the oscillations.

## discussion

Based on old and new experimental data, we have constructed a new model of the type-III  $\text{IP}_3\text{R}$  and incorporated it into a whole-cell model for intracellular  $\text{Ca}^{2+}$  oscillations in pancreatic acinar cells. This model agrees with recent data on the rates of activation and inactivation of the  $\text{IP}_3\text{R}$  by  $\text{Ca}^{2+}$  (Dufour et al., 1997), and can reproduce both the short-period, raised baseline oscillations induced by ACh in pancreatic acinar cells, as well as the long-period baseline spiking induced by CCK. The steady state open probability of the model  $\text{IP}_3\text{R}$  is a monotonically increasing function of  $[\text{Ca}^{2+}]_i$ , as shown experimentally by Hagar et al. (1998).

The ability of the model to reproduce this wide variety of experimental data is based principally on two things. (a) Physiological concentrations of CCK cause rapid phosphorylation of the  $\text{IP}_3\text{R}$  while physiological concentrations of ACh do not. Phosphorylation of the  $\text{IP}_3\text{R}$  does not appear to be  $\text{Ca}^{2+}$  dependent, and can

also result from the addition of CPT-cAMP. Hence, we hypothesize that CCK, via production of cAMP and activation of PKA, shunts the  $\text{IP}_3\text{R}$  through a phosphorylation pathway that prevents rapid recovery from receptor inactivation. Inactivation of the  $\text{IP}_3\text{R}$  by  $\text{Ca}^{2+}$  is rapid, as indicated by the data of Dufour et al. (1997), and then receptor phosphorylation holds the receptor in an inactivated state. The resulting long-period oscillations are then governed by the time taken to recover from the phosphorylated state. In the absence of phosphorylation (i.e., after stimulation by ACh), the oscillation period is governed principally by the rate of recovery from  $\text{Ca}^{2+}$ -induced inactivation of the receptor. (b) In the presence of ACh, the flux of  $\text{Ca}^{2+}$  in both directions across the plasma membrane is greater than in the presence of CCK. Measurement of the rates of  $\text{Ca}^{2+}$  removal during the downstroke of the oscillations indicates that the rate of  $\text{Ca}^{2+}$  ATPase activity is much greater in the presence of ACh than in the presence of CCK. Furthermore, it appears that ACh increases the rate of  $\text{Ca}^{2+}$  entry from outside the cell much more than does CCK. Indirect evidence for this has appeared before; Yule et al. (1991) showed that removal of external  $\text{Ca}^{2+}$  abolishes ACh-induced oscillations, but has little effect on CCK-induced oscillations. By making this assumption in the model, we were able to predict the effect of both reducing external  $\text{Ca}^{2+}$  and increasing

agonist concentration. The fact that the model predictions were confirmed by the experimental data lends support to this hypothesis, although this evidence is still indirect.

It has been known for some years that PKA is able to phosphorylate the IP<sub>3</sub>R; more recently, Wojcikiewicz and Luo (1998) have shown that type-I, -II, and -III receptors are differentially susceptible to phosphorylation in intact cell lines (AR4-2J rat pancreatoma and RINm5F rat insulinoma cells). Furthermore, it is also known that CCK activates both the adenylate cyclase and phospholipase C pathways in pancreatic acinar cells, while ACh does not appear to activate the adenylate cyclase pathway (Schulz, 1989; Petersen and Wakui, 1990). However, what is far less clear is the exact effect of IP<sub>3</sub>R phosphorylation. In some cell types, it appears that phosphorylation of the IP<sub>3</sub>R by PKA inhibits Ca<sup>2+</sup> release (Supattapone et al., 1998; Volpe and Alderson-Lang, 1990), while in hepatocytes the opposite effect occurs (Hajnoczky et al., 1993; Joseph and Ryan, 1993). In platelets, PKA phosphorylation of the IP<sub>3</sub>R causes a 30% inhibition of IP<sub>3</sub>-induced Ca<sup>2+</sup> release (Quinton and Dean, 1992), while more recent data shows that PKA inhibits IP<sub>3</sub>-induced Ca<sup>2+</sup> release in megakaryocytes (Tertyshnikova and Fein, 1998). In a renal epithelial cell line, kinase activators and phosphatase inhibitors decrease the response to carbachol, while kinase inhibitors increase the response to carbachol (Xu et al., 1996a), results that are consistent with the assumptions of our model.

Our experiments on the phosphorylation of the IP<sub>3</sub> receptor were performed in both rats and mice, and similar results were obtained. Thus it is reasonable to assume that the model of the IP<sub>3</sub> receptor is applicable to both rats and mice. However, there are quantitative differences between the Ca<sup>2+</sup> responses of rat and mice pancreatic acinar cells to agonist stimulation. In the study of Tsunoda et al. (1990) in rat pancreatic acinar cells in intact acini, Ca<sup>2+</sup> responses to application of CCh took the form of low period baseline spiking, similar to the responses to application of CCK. Since most of the studies showing clear differences between the responses to CCK and ACh have been performed in single isolated mouse pancreatic acinar cells (Osipchuk et al., 1990; Yule et al., 1991; Petersen et al., 1991a; Lawrie et al., 1993; Thorn et al., 1993b), it is not clear whether our conclusions are also applicable to rat pancreatic acinar cells in an acinus. For a start, it is known that gap junctional communication modulates the observed Ca<sup>2+</sup> oscillations in rat pancreatic acini (Stauffer et al., 1993), but whether this is sufficient to account quantitatively (or even qualitatively) for the differences in the responses of coupled and isolated cells is not known. Furthermore, it is likely that variations in crucial parameter values, such as pumping and influx

rates, will lead to quantitatively different model behavior, and such differences may be one way to explain the differing responses of rat and mice pancreatic acinar cells. However, we have not done exhaustive parameter studies and so cannot say for certain. Note, however, that baseline spiking in response to application of ACh is also seen in mouse pancreatic acinar cells, as long as the concentration of ACh is low enough. Hence, our model is consistent with the data from rat pancreatic acinar cells in this low concentration limit. It is thus plausible that the basic mechanisms are similar in both rat and mice pancreatic acinar cells, differing only in the details of certain parameter values.

In our model, we have assumed that phosphorylation of the IP<sub>3</sub>R shunts it into a closed state; it is important to note that this is assuming that phosphorylation neither inhibits nor potentiates Ca<sup>2+</sup> release. Hence, the assumptions underlying our model are consistent with both effects of PKA. This can easily be seen by the following argument. If  $k_3$  were small, then the intrinsic recovery of the IP<sub>3</sub>R from the inactivated state would be slow; if the rates of phosphorylation and dephosphorylation ( $k_4$  and  $k_5$ ) were large enough, it is possible that shunting the receptor through the phosphorylated I<sub>2</sub> state could increase the steady state open probability. Conversely, if  $k_3$  were large, and thus the intrinsic recovery from inactivation was fast, then shunting the receptor through the phosphorylated state could decrease the steady state open probability. In fact, we can derive an explicit relationship between  $k_3$ ,  $k_4$ , and  $k_5$  that will determine the exact effects of phosphorylation on the steady state open probability. The steady state proportion of open receptors,  $O$ , can be easily calculated as

$$O = \frac{\phi p}{\frac{k_{-1} + k_2}{k_1} \phi + p}, \quad (9)$$

where

$$\phi = \frac{1}{1 + \frac{k_2}{k_3 + k_4} \left(1 + \frac{k_4}{k_5}\right)}. \quad (10)$$

Thus, the function  $\phi$  controls the sensitivity of the IP<sub>3</sub>R to IP<sub>3</sub>; as  $\phi$  increases, the sensitivity of the IP<sub>3</sub>R decreases, and vice versa. A short calculation now shows that  $\phi$  is an increasing function of  $k_4$  when  $2k_3 > k_5 - k_4$ , and is a decreasing function of  $k_4$  when  $2k_3 < k_5 - k_4$ . It follows that, depending on the values chosen for  $k_3$ ,  $k_4$ , and  $k_5$ , the model can reproduce either an increase or a decrease of sensitivity of the IP<sub>3</sub>R upon phosphorylation.

Oscillations in the model occur for constant [IP<sub>3</sub>], and are the result of cycles of activation and inactivation of the IP<sub>3</sub>R. At present, there is no direct evidence

for our assumption that oscillations in  $[IP_3]$  are not necessary to obtain  $[Ca^{2+}]_i$  oscillations. From experiments using nonmetabolizable analogs of  $IP_3$ , there is indirect evidence that the observed  $[Ca^{2+}]_i$  oscillations are not governed by underlying oscillations in  $[IP_3]$  (Wakui et al., 1989; Thorn et al., 1993b). However, a complete resolution of this question awaits an experimental determination of the kinetic behavior of  $[IP_3]$  during the course of a  $[Ca^{2+}]_i$  oscillation. During application of an agonist,  $[IP_3]$  will certainly rise and fall as  $IP_3$  is produced and degraded. We do not build these features into our model directly, but just assume that  $IP_3$  is produced and degraded with given rates. Thus, in the simulations,  $[IP_3]$  increases and decreases gradually. This has little effect on the oscillatory behavior of the model, which can be well understood by considering the behavior at fixed  $[IP_3]$ .

Although it appears that ryanodine receptors do exist in pancreatic acinar cells, we have not included in the model any possible effects of ryanodine receptors or  $IP_3$ -independent  $Ca^{2+}$ -induced  $Ca^{2+}$  release. Kasai et al. (1993) have shown that the response to ACh is eliminated by heparin, although there is still  $Ca^{2+}$ -induced  $Ca^{2+}$  release from the granular area. Thus, although it is likely that  $IP_3$ -independent factors are important for modulating the shape of the  $[Ca^{2+}]_i$  oscillations, it appears that they cannot, by themselves, support oscillations. Nathanson et al. (1992) have also shown that  $Ca^{2+}$ -induced  $Ca^{2+}$  release has an effect on the speed of ACh and CCK-stimulated intracellular  $[Ca^{2+}]_i$  waves. However, neither caffeine nor ryanodine eliminates the waves, although they do decrease the wave speed. Furthermore, the intracellular waves are initiated at the apical zone of the cell, which is where the type-III  $IP_3$  receptors are mostly found (Nathanson et al., 1994). We interpret these results to mean that the oscillatory period and other fundamental oscillation properties are determined primarily by the properties of the  $IP_3$  receptors in the apical zone, with other forms of  $Ca^{2+}$ -induced  $Ca^{2+}$  release playing only a modulatory role. Hence, for simplicity, in this model we consider only  $IP_3$  receptors.

One major difference between our model and previous ones is in the assumption of how  $Ca^{2+}$  affects the  $IP_3$  receptor. Rather than assuming actual  $Ca^{2+}$  binding sites on the receptor (which are not well characterized), we assume that the actions of  $Ca^{2+}$  arise from its effect on  $IP_3$  binding. Thus, although  $[IP_3]$  is constant during an oscillation,  $IP_3$  nevertheless plays an active dynamic role, as oscillations in  $[Ca^{2+}]_i$  are driven by cycles of  $IP_3$  binding and unbinding from the receptor. In the case of CCK-induced oscillations, the receptor also undergoes periodic cycles of phosphorylation and dephosphorylation; the oscillation period is then set by the rate of receptor dephosphorylation, rather than by

the rate of receptor recovery from inactivation. Calcium-induced calcium release also plays an important role. As  $[Ca^{2+}]_i$  increases, the rate of  $IP_3$  binding to the receptor is increased (S to O transition), leading to an effective calcium activation of the receptor.

Another major difference from previous models is our use of the phosphorylation pathway, through which some agonists will shunt the receptor. It has been recognized for some time that a third mechanism, in addition to  $Ca^{2+}$  activation and inactivation of the  $IP_3R$ , is required to explain the long interspike intervals that occur in some cells (see, for example, Oancea and Meyer, 1996, for an excellent discussion of this). Indeed, phosphorylation and dephosphorylation of the  $IP_3R$  has previously been proposed as a possible mechanism for setting the interspike interval (Cameron et al., 1995; Zhu et al., 1996; in these papers, the phosphorylation was assumed to be  $Ca^{2+}$  dependent, which it does not appear to be in our cell type). We have shown that such a hypothesis is quantitatively consistent with the observed oscillations, we have collected experimental data that show agonist-dependent rates of phosphorylation of the  $IP_3$  receptor and have shown that a single mechanism can be used as a framework to understand widely differing experimental results in a single cell type. Ours is not the first model to generate long interspike intervals. Laurent and Claret (1997) constructed a model of Monod-Wyman-Changeux type and showed that, with appropriate choices of the parameters, the model could reproduce long-period oscillations, while Dupont and Swillens (1996) postulated the existence of an intermediate  $Ca^{2+}$  domain around the mouth of the receptor to achieve a similar result. Our model differs from these in that we present a single mechanism that can generate a wide variety of oscillatory patterns, and then show experimentally that the necessary elements of the model exist in a particular cell type.

The simplicity of our model can, in some circumstances, be a disadvantage. Our assumption of independent subunits is unlikely to be correct (as pointed out by Laurent and Claret, 1997), and a more detailed allosteric model of the effects of  $Ca^{2+}$  on  $IP_3$  binding would presumably increase the model's accuracy. However, we believe that the additional complications introduced by such procedures are unlikely to be a worthwhile expenditure of effort at this stage. More detailed models of the receptor states and phosphorylations can wait until the properties of the pancreatic acinar  $IP_3$  receptors are known in more detail, and until spatial effects are better understood.

Zhu et al. (1996) have presented a qualitative model that, in many respects, is similar to ours. They conclude that histamine-stimulated  $Ca^{2+}$  oscillations in HeLa cells result from cycles of phosphorylation and dephosphorylation of the  $IP_3R$  by CaMK-II. In their model, just



as in ours, phosphorylation of the IP<sub>3</sub>R inhibits Ca<sup>2+</sup> release by closing the channel. They showed that inhibition of the phosphatase by calyculin A or okadaic acid (which corresponds to a reduction in  $k_5$  in our model) increases the oscillation period, and this result is reproduced by our model (computations not shown). This emphasizes the importance of receptor dephosphorylation for setting the period of CCK-induced oscillations. In addition, our model is easily adapted to simulate phosphorylation of CaMK-II by letting  $k_4 = c^4 / (0.5^4 + c^4)$ . This assumes that phosphorylation by CaMK-II is modulated by Ca<sup>2+</sup> in a cooperative fashion, and thus includes the possibility of feedback from the Ca<sup>2+</sup> signal to receptor phosphorylation. In this case, the model again exhibits long-period baseline spiking (computations not shown).

One principal feature of our model that is supported only indirectly is the assumption that ACh increases membrane transport of Ca<sup>2+</sup>, while CCK increases it to a lesser extent. In other words, when the cell is at steady state (i.e., in the absence of agonist stimulation) there is a continual, but small, flux of Ca<sup>2+</sup> through the cytoplasm, as Ca<sup>2+</sup> leaks into the cell and is quickly removed. Upon ACh stimulation, overall membrane transport of Ca<sup>2+</sup> is greatly increased, in both directions, and this, in combination with activation of the IP<sub>3</sub>R, results in raised-baseline, sinusoidal, oscillations that are dependent on external Ca<sup>2+</sup>. CCK, on the other hand, increases membrane transport of Ca<sup>2+</sup> only slightly, and thus CCK-induced oscillations depend on external Ca<sup>2+</sup> much less. It has been known for some years that the rate of Ca<sup>2+</sup> turnover is low at steady state, and that agonists such as CCh and CCK increase the rate of Ca<sup>2+</sup> pumping out of the cytoplasm, as well as increasing the rate of Ca<sup>2+</sup> influx (Muallem and Beeker, 1989; Zhang et al., 1992). However, what is not clear is whether ACh increases the rate of Ca<sup>2+</sup> turnover more than does CCK. Our model makes the assumption that it does. Although we used our model to make predictions about the effects of removing external Ca<sup>2+</sup> and subsequently increasing [ACh], and these predictions were confirmed experimentally, and although the model provides a consistent framework that can possibly explain the different effects of low extracellular Ca<sup>2+</sup> on ACh- or CCK-induced oscillations, this is still only indirect evidence for this assumption. One important test of the model will be to compare transmembrane and trans-ER Ca<sup>2+</sup> fluxes directly, in the presence of CCK or ACh, or neither.

Lawrie et al. (1993) have shown that application of ACh in the absence of external Ca<sup>2+</sup> will initially cause oscillations, but these die away within a few minutes. This particular result is not reproduced by our model because of the simplified way in which it treats Ca<sup>2+</sup> pumping. When Ca<sup>2+</sup> is removed from the cytoplasm

by pumps, it can be removed either to the outside or to the ER. It is easy to see that the rate of removal to the ER has no effect on the long term steady state  $[Ca^{2+}]_i$  of the cell, which can only be affected by Ca<sup>2+</sup> transport across the plasma membrane. When ACh is applied to a cell in low  $[Ca^{2+}]_i$ , the kinetics of the IP<sub>3</sub>R can still lead to cycles of Ca<sup>2+</sup> release and uptake from the ER, but each time Ca<sup>2+</sup> is released into the cell cytoplasm, a fraction of it is lost to the outside. Eventually, the cell runs down and oscillations stop, as observed. Thus, over a longer time scale, depletion of the ER plays a role in terminating Ca<sup>2+</sup> oscillations. The only way to model this is to treat Ca<sup>2+</sup> transport across the ER membrane separately from Ca<sup>2+</sup> transport across the plasma membrane, a feature that is omitted from our model for the sake of simplicity. However, we have constructed an extended version of the model, in which we take into account depletion of the ER (LeBeau, Yule, and Sneyd, unpublished data). The extended model behaves in a similar manner to the model presented here, but can account for a wider array of experimental results, including long-time oscillatory behavior and the application of ACh in the absence of external Ca<sup>2+</sup>. Details of this model and comparison with experimental results will be presented in a later paper.

Another important feature of the model is the assumption that an increase in  $[Ca^{2+}]_i$  causes an increase in the binding affinity of IP<sub>3</sub> to its receptor. The experimental data on the properties of IP<sub>3</sub> binding as a function of Ca<sup>2+</sup> are not completely consistent. Yoneshima et al. (1997) claim that Ca<sup>2+</sup> increases the binding affinity of IP<sub>3</sub> to type-III receptors, but decreases the binding affinity to type-I receptors. However, Cardy et al. (1997), although agreeing that the major effect of Ca<sup>2+</sup> on IP<sub>3</sub> binding is stimulatory for type-III and inhibitory for type-I receptors, claim that these effects are mediated by changes in the maximal binding (although, for type-III receptors, more complex effects occur at higher Ca<sup>2+</sup> concentrations). Nevertheless, they conclude that Ca<sup>2+</sup> regulates the interconversion of the IP<sub>3</sub>R between two different states, one state with a high IP<sub>3</sub> affinity, and the other with a low affinity. This interpretation is entirely consistent with our results, as our model can in fact be rigorously derived by considering just such a receptor mechanism (Sneyd, LeBeau, and Yule, manuscript submitted for publication).

As we show in the APPENDIX, a decrease in IP<sub>3</sub> binding affinity with increasing Ca<sup>2+</sup> implies that the peak of the steady state open probability curve shifts to the right as  $[IP_3]$  increases. Conversely, an increase in the IP<sub>3</sub> binding affinity with increasing Ca<sup>2+</sup> implies that the steady state open probability curve will shift to the left with increasing  $[IP_3]$ . Thus, since type-I receptors have a decreasing IP<sub>3</sub> binding affinity with increasing Ca<sup>2+</sup>, the model predicts that the steady state open

probability curve will shift to the right with increasing  $[IP_3]$ , exactly as seen by Kaftan et al. (1997). On the other hand, since type-III receptors have an increasing  $IP_3$  binding affinity with increasing  $Ca^{2+}$ , we predict that the steady state open probability curve will shift to the left with increasing  $[IP_3]$ . These measurements have yet to be performed. No models to date (at least that we know of) have investigated the effects of changes in the maximal binding. In this context, it is important to note that the open probability curve at infinite  $[IP_3]$  does not give the maximal binding curve. In our model (and all other receptor binding models that we have investigated), the maximal binding fraction is always 1 and, as in the presence of large amounts of  $IP_3$ , all receptors will bind  $IP_3$ .

As well as the temporal responses to ACh and CCK being quite different, the spatial characteristics of the response are also agonist dependent (Lawrie et al., 1993; Thorn et al., 1993a; Xu et al., 1996b). ACh-induced oscillations are initiated at the secretory pole of the cell, and spread from there across the cell, with the response at the basal pole being consistently of smaller amplitude and slightly delayed. During the course of this intracellular wave, significant  $Ca^{2+}$  gradients are maintained in the cell cytoplasm. CCK, on the other hand, causes an increase in  $[Ca^{2+}]_i$  that is simultaneous across the entire cell, with no change in amplitude from secretory to basal poles. Furthermore, these intracellular  $Ca^{2+}$  waves can be transmitted intercellularly when individual cells in acini are coupled to their neighbors via gap junctions (Yule et al., 1996). A prerequisite for the study of such intra- and intercellular waves is a detailed understanding of the kinetics underlying the oscillatory response in each individual cell. Thus, although the current study does not address these questions, our model provides a useful framework that can be used to study the problem of wave propagation in this cell type.

## appendix

### The Steady State Open Probability of the $IP_3R$

In the majority of current models of the  $IP_3R$ , the steady state receptor open probability,  $O$ , can be expressed in the general form

$$O = \frac{\theta_1(c)p}{p + \theta_2(c)} \quad (11)$$

for some functions  $\theta_1$  and  $\theta_2$ . The exact form of these two functions differs from model to model. However, we note two things. First,  $p = \theta_2(c)$  gives the half-maximal  $IP_3$  binding to the receptor, and thus  $\theta_2(c)$  is the  $EC_{50}$  of the  $IP_3$  receptor, with respect to  $IP_3$  binding. It thus follows from experimental data (Yoneshima et al.,

1997) that, for type-I receptors,  $\theta_2$  is an increasing function of  $Ca^{2+}$ , while for type-III receptors,  $\theta_2$  is a decreasing function of  $Ca^{2+}$ . Secondly,  $\theta_1(c)$  is the open probability as a function of  $c$ , when  $p$  is very large; i.e., in the limit of high  $[IP_3]$ .

### Bell-shaped Steady State Curve

If  $O$  is a bell-shaped function of  $c$ , it follows that it must have a turning point, at which place  $\frac{\partial O}{\partial c} = 0$ . Hence, at the turning point,

$$(p + \theta_2)\theta'_1 = \theta_1\theta'_2. \quad (12)$$

If we let  $c_0$  denote the position of the turning point, then Eq. 12 can be solved to obtain  $c_0 = c_0(p)$ . We want to know whether  $c_0$  is an increasing or decreasing function of  $p$ . In other words, does the peak of the bell-shaped curve move to the right or to the left as  $p$  increases.

First, we note that an implicit differentiation gives

$$c'_0(p) = \frac{\theta'_1}{\theta_1\theta'_2 - \theta_2'(p + \theta_2)}. \quad (13)$$

It thus follows that the only way  $c'_0(p)$  can change sign is if  $\theta'_1(c_0)$  changes sign. [We do not let the denominator change sign, because if it did, then  $c'_0(p)$  would become infinite, which is clearly unphysiological. For the same reason, we also exclude singular cases, where both the numerator and denominator vanish together.] Finally, we note that, at the turning point,  $p + \theta_2 = \theta_1\theta'_2/\theta'_1$ , and so, from Eq. 11, it follows that the open probability at the turning point,  $O_{tp}$ , is given by

$$O_{tp} = \frac{\theta_1\theta'_1 p}{\theta_1\theta'_2} = \frac{\theta'_1 p}{\theta'_2}. \quad (14)$$

We know that, for type-I receptors,  $\theta_2$  is an increasing function of  $c$ . Hence, for this receptor type,  $\theta'_2 > 0$ . From Eq. 14, it now follows that  $O_{tp}$  is positive only when  $\theta'_1 > 0$  at the turning point. However, recall that  $\theta_1$  is just the open probability curve at high  $p$ . Hence, for lower values of  $p$ , the peak of the open probability curve must occur at values of  $c$  for which  $\theta'_1 > 0$ . Since  $\theta'_1$  cannot change sign, neither can  $c'_0(p)$ . It remains only to determine which sign it is. However, it is easy to see that, when  $p$  is large,  $c'_0(p)$  must be positive. Hence,  $c'_0(p)$  is always positive for all  $p$ , from which it follows that the peak of the bell-shaped curve must move to the right as  $p$  increases. [It is interesting to note that the same argument works when  $\theta_2$  is a decreasing function of  $c$ , and thus  $\theta'_2 < 0$ . In this case,  $c'_0(p)$  is always negative for all  $p$ , from which it follows that the peak of the bell-shaped curve must move to the left as  $p$  increases.]

### Monotonic Steady State Curve

Type-III receptors do not have bell-shaped steady state open probability curves, and thus the above argument

does not apply to them. However, a similar argument can be used to show that the steady state open probability curve (i.e., the point of maximum slope) shifts to the left as  $p$  increases.

Suppose the steady state open probability curve is monotonically increasing, and define

$$\theta_1^{\max} = \lim_{c \rightarrow \infty} \theta_1(c), \quad (15)$$

$$\theta_2^{\max} = \lim_{c \rightarrow \infty} \theta_2(c). \quad (16)$$

For a fixed value of  $p$ , the steady state open probability curve,  $O$ , reaches half its maximum value at the point  $c_0$ , where  $c_0$  is found by solving the equation

$$\frac{\theta_1(c_0)p}{p + \theta_2(c_0)} = \frac{1}{2} \cdot \frac{\theta_1^{\max} p}{p + \theta_2^{\max}}. \quad (17)$$

Note that this defines  $c_0$  as a function of  $p$ ; i.e.,  $c_0(p)$ . We now want to find out whether  $c_0$  is an increasing function of  $p$  (in which case the curves shift to the right as  $p$  increases), or a decreasing function of  $p$  (in which case the curves shift to the left as  $p$  increases).

Differentiate both sides with respect to  $p$  to get

$$\frac{dc_0}{dp} = \frac{\theta_1 - \frac{\theta_1^{\max}(p + \theta_2)^2}{(p + \theta_2^{\max})^2}}{\theta_1'(p + \theta_2) - \theta_1\theta_2'}, \quad (18)$$

where all functions of  $c$  are evaluated at  $c_0$ .

For a type-III receptor,  $\theta_2'(c) < 0$  (as argued above), and we also suppose that the steady state open probability curve is monotonic for all  $IP_3$  concentrations and thus  $\theta_1'(c) > 0$ . If, for any  $p$ , the steady state curve becomes bell-shaped, the previous argument applies. Since

$$\theta_1 - \theta_1^{\max} \frac{(p + \theta_2)^2}{(p + \theta_2^{\max})^2} < 0, \quad (19)$$

it now follows that  $\theta_2^{\max} < \theta_2(c)$ , and  $\theta_1^{\max} > \theta_1(c)$ , and thus  $c_0'(p) < 0$ .

In conclusion, we have predicted that, as  $p$  increases, the steady state open probability curve of a type-III  $IP_3R$  will move to the left. To our knowledge, this has not yet been experimentally measured.

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